

AFAPL-TR-79-2077

DETERMINATION OF FLOW DIRECTION WITH PRESSURE PROBES

G.D. HUFFMAN Purdue University West Lafayett, Indiana 47907

D.C. RABE

N.D. POTI

U.S. Air Force Aero Propulsion Laboratory Wright-Patterson Air Force Base, Ohio 45433

D.N. BARLOW
U.S. Air Force Academy
Colorado Springs, Colorado 80840

SEPTEMBER 1980

TECHNICAL REPORT AFAPL-TR-79-2077

Final Report for Period 1 June 1978 - 1 July 1979

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DOUGLAS & RABE

Aerospace Engineer

Compressor Test Group

Technology Branch

DR. FRANCIS R. OSTDIEK

Chief, Compressor Test Group

Technology Branch

FOR THE COMMANDER

Deputy Director

Turbine Engine Division Aero Propulsion Laboratory

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AIR FORCE/56780/3 November 1980 - 70

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered) READ INSTRUCTIONS REPORT DOCUMENTATION PAGE BEFORE COMPLETING FORM 3. RECIPIENT'S CATALOG NUMBER GOVT ACCESSION NO. AFAPL-TR-79 -2Ø77 AD-11092028 TITLE (and Subtitle) Jun/78 -1 Jul 79 DETERMINATION OF FLOW DIRECTION WITH PRESSURE 6. PERFORMING ORG. REPORT NUMBER PROBES AUTHOR(s) 8. CONTRACT OR GRANT NUMBER(s) AFOSR Grant IPA-808-78-G. David/Huffman, Purdue University 01010 Rabe / N./Poti D. N./Barlow, 🛣 -Academy PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS AF Aero Propulsion Laboratory Program Element - 646100 FJ Seiler Research Laboratory Project-3066, Task-306617 AF Academy Work Unit - 30661740 11. CONTROLLING OFFICE NAME AND ADDRESS QRI.DATE Jul. 1979, Air Force Aero Propulsion Laboratory 13. NUMBER OF PAGES Air Force Wright Aeronautical Laboratories 85 Wright-Patterson Air Force Base, Ohio 45433 15. SECURITY CLASS, (of this report) UNCLASSIFIED 15a. DECLASSIFICATION DOWNGRADING SCHEDULE 16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Cone Probes Pressure Probes Flow Direction Measurement \$lender Body Theory RACT (Continue on reverse side if necessary and identify by block number) This report documents the results of a theoretical and experimental study of flow direction probes for use in turbomachines. The theoretical analyses

This report documents the results of a theoretical and experimental study of flow direction probes for use in turbomachines. The theoretical analyses employ slender body theory with the resulting expressions converted into angular and averaged pressure coefficients. These are in turn used to quantify the effects of probe geometry on probe sensitivity. Furthermore, the analytic expressions are employed to predict the impact of probe alignment on the angular and averaged pressure coefficients.

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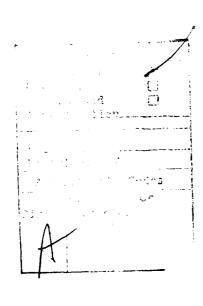
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### 20. Abstract

In addition to the analytic studies, an experimental evaluation of a typical flow direction probe is also presented. Measurements are carried out over a series of Mach numbers and angle of attack and sideslip angles. Angular, averaged and total pressure coefficients are determined from the measured pressures for Mach numbers of from 0.05 to 0.80 and angles of attack from -20° to 20° and sideslip angles from 0° to 20°.

The theoretical results are compared to two sets of experimental data. The first consists of measurements made using a large cone model and the second is made up of the data taken in the current study. The qualitative trends with Mach number and flow angles are the same in both cases and are well reproduced by the theory. Quantitatively the data taken on the large cone agrees well with the theory while the data from the miniature flow-direction probe tends to differ from the analytic predictions. The divergence may be due to shape and pressure tap anomalies introduced in the manufacturing process.



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## LIST OF SYMBOLS

| Symbol               | Definition  | Units               |
|----------------------|---|---------------------|
| с                    | Speed or sound  | m/sec               |
| C <sub>p</sub>       | Pressure coefficient                                      |                     |
| Δcp                  | Difference of pressure coefficient                        |                     |
| <c<sub>p&gt;</c<sub> | Averaged pressure coefficient                             |                     |
| d                    | Diameter  | m or mm             |
| f                    | Body geometry function                                    |                     |
| g                    | Source distribution per unit length for lateral flow      | m²/sec              |
| М                    | Mach number   |                     |
| p                    | Pressure  | $n/m^2$             |
| >                    | Average pressure  | n/m²                |
| q                    | Source distribution per unit length for axisymmetric flow | m <sup>2</sup> /sec |
| r,θ,z                | Cylindrical coordinates                                   | m, Degrees          |
| R                    | Body radius   | m                   |
| Re                   | Reynolds number   |                     |
| S                    | Body cross-sectional area                                 | $\mathfrak{m}^2$    |
| t                    | Time  | sec                 |
| v                    | Perturbation velocity                                     | m/sec               |
| V                    | Velocity  | m/sec               |
| x,y,z                | Cartesian coordinates                                     | m                   |
| α                    | Angle of attack   | Degrees             |
| β                    | Cross-flow angle  | Degrees             |
| δ                    | $\sqrt{1-M}$  |                     |
| $\delta_{f c}$       | Probe half angle  | Degrees             |
| ej                   | Angle of decrease of jet potential cone                   | Degrees             |
| p<br>p               | Density   | kg/m <sup>3</sup>   |
| Φ                    | Perturbation potential                                    | m²/sec              |
| Φ                    | Potential function  | m²/sec              |

## LIST OF SUBSCRIPTS

| Subscript | Detinition             |
|-----------|------------------------|
| t         | Total                  |
| ω         | Free-stream conditions |
| o         | Reference state        |
| i         | Probe center port      |
| 2,3,4,5   | Probe side ports       |

### LIST OF SUPERSCRIPTS

| Superscript | <u>Definition</u>                           |  |
|-------------|---|--|
| n           | Nozzle                                      |  |
| P           | Probe                                       |  |
| r, θ, z     | Cylindrical coordinates                     |  |
| x, y, z     | Cartesian coordinates                       |  |
| i.          | Axisymmetric flow past a body of revolution |  |
| 2           | Lateral flow past a body of revolution      |  |

#### SECTION I

#### INTRODUCTION

Turbomachine flow fields are three-dimensional with a variation in flow direction, flow velocity, temperature and pressure occurring in both the radial and circumferential directions. The temperatures, pressures and turbulence levels encountered necessitate both simple and structurally sound probes and/or sensors. The harsh turbomachine environment makes multi-ported, pressure probes particularly attractive for measurement of flow direction.

Pressure probes usually consist of aerodynamic shapes with a symmetrical arrangement of sensing holes. A number of different geometries have been investigated and some typical cases are reviewed in references 1 through 15. A more general treatment of probes is given in references 16 and 17.

Pressure probes are normally employed in either the stationary or nulling mode. In the nulling or equal pressure mode, the probe is oriented such that each of the side ports, see Figure 1 for instance, reads the same pressure. The probe position is noted and the flow direction determined. In the stationary mode, the probe is fixed and the top-to-bottom and side-to-side pressure differences are noted. Calibration functions are then used to find  $\alpha$  and  $\beta$ . The static and total pressures can also be determined in a similar manner.

Both methods offer advantages and disadvantages. The nulling technique tends to be the most accurate. The probe can be designed for maximum sensitivity at small angles. It offers the disadvantage, however, of considerable mechanical complexity particularly in three-dimensional flow fields. The stationary probe method, while mechanically superior to the nulling approach, tends to be less accurate, especially at large flow angles. Despite the accuracy of the nulling technique, this technique is considered inappropriate for turbomachine measurements because of its related mechanical complexity. Consequently, only stationary probes are considered in this work.

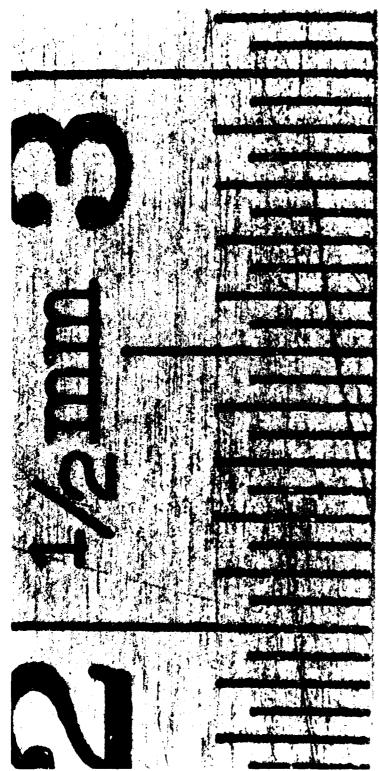




Figure 1. Typical Flow Direction Probe

Since the probes are to be used without rotation, the sensitivity to flow angularity is extremely important. While values of this parameter are available for a number of calibrated probes, this data is only of limited value in synthesizing a probe geometry yielding a desired angular sensitivity. Therefore, a general analytic model has been developed using slender body theory and this is discussed in Section 2.

In order to verify the analysis as well as calibrate a series of probes for use in an upcoming compressor test, the angular, static and total pressure sensitivities for a five-ported, conical probe have been determined experimentally. These tests are discussed in Sections 3 and 4. The results of the measurements are compared with the mathematical model of Section 2 in Section 5.

In addition to the probe sensitivity which is largely dictated by aerodynamic considerations, alignment and manufacturing defects also influence the accuracy with which flow angles and static and total pressures can be determined. Effects of this nature are discussed in Section 6. Some optimum probe geometries are also postulated.

### SECTION II

### A MATHEMATICAL MODEL OF PROBE AERODYNAMIC BEHAVIOR

### 2.1 Objectives

The objective of an aerodynamic probe - in the present context - is to determine the magnitude and direction of the velocity vector. This translates into a measurement of pressures which - by means of calibration functions - are then converted into flow angles and total and static pressures. The flow field parameters should be accurately measured with the probe, itself, creating a minimal flow disturbance. The probe must also be structurally sound - the last two requirements are somewhat at variance.

A typical flow direction probe having an "aerodynamic shape" can be thought of as a slender body, i.e., the body radius is much less than the body length. The use of slender body theory in the analysis of aerodynamic probes, thus, immediately comes to mind. There are, however, shortcomings associated with this approach. The major one being that the rate of change of body radius with respect to body length must also be small. This feature precludes stagnation points in a slender body approach.

Of course, a complete description of the flow field around an aero-dynamic probe can be generated by numerically solving the three-dimensional potential flow equations, see, for instance, references 18 and 19. While this approach is more accurate than stender body theory, it does not lend itself to synthesis or probe shapes. Furthermore, analytic calibration relations are not obtained and considerable insight into the physical processes is lost. Consequently, slender body analysis will be employed in the ensuing analysis.

### 2.2 Basic Formulation of Slender Body Theory

A slender body of revolution in a cross-flow is shown in Figure 2. The body itself can be described in terms of axial, z, and radial, r, coordinates with

$$r = R(z) \tag{1}$$

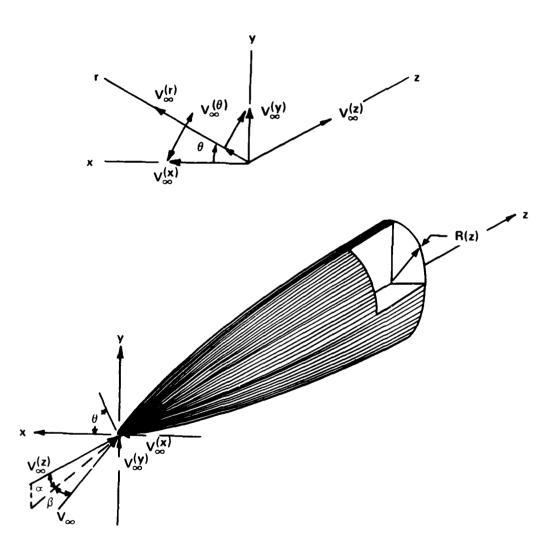


Figure 2. Slender Body of Revolution in a Cross-Flow

Following Shapiro, reference 20, the differential equation for the velocity potential,  $\Phi$ , can be written as

$$\left(1 - \frac{\Phi_{r}^{2}}{c^{2}}\right) \Phi_{rr} + \left(1 - \frac{\Phi_{\theta}^{2}}{r^{2}c^{2}}\right) \frac{\Phi_{\theta\theta}}{r^{2}} + \left(1 - \frac{\Phi_{z}^{2}}{c^{2}}\right) \Phi_{zz} - 2 \frac{\Phi_{z}\Phi_{r}}{c^{2}} \Phi_{zr}$$

$$-2\frac{\Phi_{\mathbf{r}}\Phi_{\theta}}{\mathbf{r}^{2}\mathbf{c}^{2}}\Phi_{\mathbf{r}\theta}-2\frac{\Phi_{\theta}\Phi_{\mathbf{z}}}{\mathbf{r}^{2}\mathbf{c}^{2}}\Phi_{\theta\mathbf{r}}+\frac{\Phi_{\mathbf{r}}}{\mathbf{r}}\left(1+\frac{\Phi_{\theta}^{2}}{\mathbf{r}^{2}\mathbf{c}^{2}}\right)=0$$
(2)

where

$$c^{2} = c_{0}^{2} - \frac{k-1}{2} \left( \phi_{r}^{2} + \frac{\phi_{0}^{2}}{r^{2}} + \phi_{z}^{2} \right)$$
 (39)

and

$$V^{(r)} = \Phi_r, \quad V^{(\theta)} = \frac{1}{r} \Phi_{\theta}, \quad V^{(z)} = \Phi_z$$
 (4)

The subscripts r,  $\theta$  and z denote partial differentiation, i.e.,

$$\Phi_{\mathbf{r}} = \frac{\partial \Phi}{\partial \mathbf{r}}$$
, etc.

Equation (2) can be rewritten in terms of a perturbation velocity potential,  $\phi$ , by expressing the potential  $\Phi$  as the sum of the perturbation due to the body and the potential due to the external flow,  $V_{\infty}$ . It then follows that

$$\Phi_{r} = V_{\infty}^{(r)} + v^{(r)} \qquad \Phi_{\theta} = r(V_{\infty}^{(\theta)} + v^{(\theta)}) \qquad \Phi_{z} = V_{\infty}^{(z)} + v^{(z)}$$
 (5)

with the perturbation potentials defined as

$$\phi_r = v^{(r)} \qquad \phi_\theta = rv^{(\theta)} \qquad \phi_z = v^{(z)} \tag{6}$$

If it is now assumed that the perturbation velocities are much smaller than the free-stream conditions, i.e.,

$$\frac{\mathbf{v}^{(r)}}{\mathbf{V}_{\infty}}, \quad \frac{\mathbf{v}^{(\theta)}}{\mathbf{V}_{\infty}}, \quad \frac{\mathbf{v}^{(z)}}{\mathbf{V}_{\infty}} << 1$$

then

$$\phi_{rr} + \frac{1}{r} \phi_{r} + \frac{1}{r^{2}} \phi_{\theta\theta} + (1 - M_{\infty}^{2}) \phi_{zz} = 0$$
 (7)

following Liepman and Roshko, reference 21. Note that  $M_{\infty} = V_{\infty}/c_{\infty}$ . The boundary conditions on the body surface can be written as

grad 
$$\Phi$$
 grad  $F = 0$  on  $F(r, \theta, z)$ 

when  $F(r, \theta, z) = r - R(z)$ . With grad  $\Phi = \overrightarrow{V}_{\infty} + \text{grad } \Phi = \overrightarrow{V}_{\infty} + \overrightarrow{v}$ , then equation (8) becomes

$$(\overrightarrow{V}_{m} + \overrightarrow{v})$$
 . grad  $F = 0$  on  $F(r, \theta, z) = 0$ 

and

$$\left[V_{\infty}^{(r)} + V^{(r)}\right] \frac{\partial F}{\partial r} + \left[V_{\infty}^{(z)} + V^{(z)}\right] \frac{\partial F}{\partial z} = 0 \quad \text{on } F(r, \theta, z) = 0 \quad (\xi)$$

The outer boundary condition is simply

$$v^{(r)}, v^{(\theta)}, v^{(z)} \rightarrow 0 \quad r \rightarrow \infty$$
 (9)

Equations (7), (8) and (9) comprise the basic relations for the perturbation flow around a slender body. The solution of equation (7) subject to the boundary conditions of equations (8) and (9) is discussed in the following section.

### 2.3 Solution of the Partial Differential Equations

The system of equations of Section 2.2 is generally solved by using superposition after subdividing the flow field into two elements - the first being the axisymmetric flow past the body of revolution and the second being the transverse and/or lateral flow past the same body. These conditions can be expressed mathematically as

$$\phi_{rr}^{(1)} + \frac{\phi_{r}^{(1)}}{r} + (1-M_{\infty}^{2}) \phi_{zz}^{(1)} = 0$$

$$\phi_{r}^{(1)} = v^{(r)} = V_{\infty}^{(z)} \frac{dR}{dz} \quad F(r,\theta,z) = 0$$
Axisymmetric Flow
$$Past \ a \ Body$$
of Revolution
$$v^{(r)}, v^{(z)} \to 0 \quad r \to \infty$$

and

$$\phi_{rr}^{(2)} + \frac{\phi_{r}^{(2)}}{r} + \frac{\phi_{\theta\theta}^{(2)}}{r^{2}} + \phi_{zz}^{(2)} = 0$$

$$v^{(r)} = -V_{\infty}^{(r)} \qquad F(r,\theta,z) = 0$$

$$V^{(r)}, v^{(\theta)}, v^{(z)} \to 0 \qquad r \to \infty$$
Lateral Flow
Past a Body
of Revolution
$$v^{(r)} = v^{(r)} + v^{(r)$$

with  $\phi = \phi^{(1)} + \phi^{(2)}$ .

Equation (10) can be written in terms of a source distribution, q(z), per unit length along the z axis following Sears, reference 22. This yields the integral equation

$$\phi^{(1)} = -\frac{1}{4\pi} \int_0^{\ell} q(\xi) \frac{d\xi}{\sqrt{(z-\xi)^2 + \delta^2 r^2}}$$
 (12)

where  $\delta = \sqrt{1-M_{\infty}^2}$ . The velocity components  $v^{(r)}$  and  $v^{(z)}$  are then given by

$$v^{(z)} = \phi_z^{(1)} = \frac{1}{4\pi\delta} \int_0^{\ell} \frac{(z-\xi)q(\xi)d\xi}{[(z-\xi) + \delta^2 r^2]^{3/2}}$$
(13)

and

$$v^{(r)} = \frac{\delta r}{4\pi} \int_0^{\ell} \frac{q(\xi) d\xi}{[(z-\xi)^2 + \delta^2 r^2]^{3/2}}$$

At this point the source distribution function  $q(\xi)$  is unspecified. In essence, an arbitrary specification of q produces an arbitrary body R(z). Presumably,  $q(\xi)$  could be systematically evaluated until the boundary conditions of equation (10) were satisfied. This is obviously unsatisfactory and an approximate technique yielding a direct solution was developed by Laitone, references 23 and 24. He presumed that  $q(\xi)$  could be written as

$$q(\xi) = q(z + \delta r \eta) = \sum_{n=0}^{\infty} \frac{(\delta r \eta)^n}{n!} q^{(n)}(z)$$

It thus follows that

$$\phi_{z}^{(1)} = -\frac{1}{4\pi\delta} \sum_{n=0}^{\infty} \frac{(\delta r)^{n-1}}{n!} f^{(n)}(z) \int_{-z/\delta r}^{(\ell-z)/\delta r} \frac{\eta^{n+1} d\eta}{(\eta^{2}+1)^{3/2}}$$

$$\phi_{r}^{(1)} = \frac{1}{4\pi\delta} \sum_{n=0}^{\infty} \frac{(\delta r)^{n-1}}{n!} f^{(n)}(z) \int_{-z/\delta r}^{(\ell-z)/\delta r} \frac{\eta^{n} d\eta}{(\eta^{2}+1)^{3/2}}$$
(14)

The integrals in equation (14) can be evaluated on a term-by-term basis

$$\phi_{z}^{(1)} = -\frac{1}{4\pi\delta} \left\{ \frac{q(z)}{z} \left[ \frac{1}{\sqrt{z^{2} + \delta^{2} r^{2}}} - \frac{1}{\sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right] - q^{*}(z) \left[ \frac{z}{\sqrt{z^{2} + \delta^{2} + r^{2}}} + \frac{\ell - z}{\sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} + \ell n \left( \frac{-z + \sqrt{z^{2} + \delta^{2} r^{2}}}{\ell - z + \sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right) \right] + q^{*}(z) \left[ \frac{z^{2}}{\sqrt{z^{2} + \delta^{2} r^{2}}} - \frac{(\ell - z)^{2}}{\sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} + 2\sqrt{(\ell - z)^{2} + \delta^{2} r^{2}} - 2\sqrt{z^{2} + \delta^{2} r^{2}}} \right] + \dots \right\}$$

$$\phi_{r}^{(1)} = \frac{1}{4\pi} \left\{ \frac{2q(z)}{\delta r} \right\}$$
(15)

for terms of order less than  $\delta r$ . q(z) can now be related to the body coordinates through the boundary condition on the body and

$$\phi_{r}^{(1)} = \frac{1}{4\pi} \left| \frac{2q(z)}{\delta R} \right| + V_{\infty}^{(z)} R'$$

where R' denotes dR/dz, etc. It thus follows that

$$q(z) = 2\pi \delta V_{\infty}^{(z)} RR' = \delta V_{\infty}^{(z)} S'$$
 (16)

where S denotes the body cross-sectional area,  $\pi R^2$ . With q(z) related to the body cross-sectional area, the velocities, i.e.,  $\phi_z^{(1)}$  and  $\phi_r^{(1)}$ , are completely defined.

The lateral flow past the body can be determined in a similar manner by noting that if  $\phi^{(1)}(r,z)$  is a solution of equation (10) then both  $\sin \theta \phi_r^{(1)}$  and  $\cos \theta \phi_r^{(1)}$  are solutions of equation (11). Using term by term integration and applying the boundary condition on the body yields

$$\phi_{\mathbf{r}}^{(2)} = \frac{V_{\infty}^{(\mathbf{x})} \cos \theta + V_{\infty}^{(\mathbf{y})} \sin \theta}{\pi} \left\{ -\frac{S}{r^2} \right\}$$

$$\phi_{\theta}^{(2)} = \frac{V_{\infty}^{(\mathbf{y})} \cos \theta - V_{\infty}^{(\mathbf{x})} \sin \theta}{\pi} \left\{ \frac{S}{r} \right\}$$

$$\phi_{\sigma}^{(2)} = \frac{V_{\infty}^{(\mathbf{x})} \cos \theta + V_{\infty}^{(\mathbf{y})} \sin \theta}{\pi} \left\{ \frac{S'}{r} \right\}$$

$$(17)$$

### 2.4 The Velocity Components and Pressure Coefficient

Equations (15), (16) and (17) can be combined to yield the perturbation velocities and

$$v^{(r)} = \frac{1}{2} V_{\infty}^{(z)} \frac{(R^2)!}{r} - (V_{\infty}^{(x)} \cos \theta + V_{\infty}^{(y)} \sin \theta) \left(\frac{R}{r}\right)^2$$

$$v^{(\theta)} = (V_{\infty}^{(y)} \cos \theta - V_{\infty}^{(x)} \sin \theta) \frac{R^2}{r^2}$$

$$v^{(z)} = \frac{1}{2} V_{\infty}^{(z)} f + (V_{\infty}^{(x)} \cos \theta + V_{\infty}^{(y)} \sin \theta) \frac{(R^2)!}{r}$$

$$(18)$$

where  $V_{\infty}^{(x)}$ ,  $V_{\infty}^{(y)}$  and  $V_{\infty}^{(z)}$  can be related to  $V_{\infty}$  through the angles  $\alpha$  and  $\beta$ . The pressure coefficient is the major concern in probe analysis and this parameter can be related to the velocities by means of

$$p = p_{\infty} + \frac{1}{2} \rho V_{\infty}^{2} \left[ 1 - \frac{V^{2}}{V_{\infty}^{2}} \right]$$
 (19)

In terms of the perturbation velocities v, the above relation becomes

$$p = p_{\infty} - \frac{1}{2} \rho V_{\infty}^{2} \left[ 2 \frac{\vec{V}_{\infty} \cdot \vec{v}}{V_{\infty}^{2}} + \frac{\vec{v}^{2}}{V_{\infty}^{2}} \right]$$

where  $\overrightarrow{v}$  is evaluated on the body surface. The pressure coefficient,  $C_{p}$  is defined as

$$C_{p} = \frac{p - p_{\infty}}{\frac{1}{2} \rho V_{\infty}^{2}} = -2 \frac{V_{\infty} \cdot V}{V_{\infty}^{2}} - \frac{V^{2}}{V_{\infty}^{2}}$$
 (20)

Following Karamcheti, reference 25,  $v^2$  can be approximated as  $[v^{(r)}]^2 + [v^{(\theta)}]^2$  and the pressure coefficient becomes

$$C_{p}V_{\infty}^{2} = [V_{\infty}^{(z)}]^{2}[-f-(R')^{2}] + [V_{\infty}^{(x)}]^{2}[1-4\sin^{2}\theta] + [V_{\infty}^{(y)}]^{2}[1-4\cos^{2}\theta] + V_{\infty}^{(z)}V_{\infty}^{(x)}[-4R'\cos\theta] + V_{\infty}^{(z)}V_{\infty}^{(y)}[-4R'\sin\theta] + V_{\infty}^{(x)}V_{\infty}^{(y)}[8\sin\theta\cos\theta]$$
(21)

and the body surface function f is

$$f = -\frac{1}{2} (R^2)' \left\{ \frac{1}{\sqrt{z^2 + \delta^2 r^2}} - \frac{1}{\sqrt{(\ell - z)^2 + \delta^2 r^2}} \right\} +$$
 (22)

$$\frac{1}{2} (R^{2})^{"} \left\{ \frac{\ell - z}{\sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} + \frac{z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \ell n \left[ \frac{-z + \sqrt{z^{2} + \delta^{2} r^{2}}}{\ell - z + \sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right] \right\} - \frac{1}{2} (R^{2})^{"} \left\{ \frac{\ell - z}{\sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} + \frac{z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \ell n \left[ \frac{-z + \sqrt{z^{2} + \delta^{2} r^{2}}}{\ell - z + \sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right] \right\} - \frac{\ell - z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \frac{\ell - z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \ell n \left[ \frac{-z + \sqrt{z^{2} + \delta^{2} r^{2}}}{\ell - z + \sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right] \right\} - \frac{\ell - z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \frac{\ell - z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \ell n \left[ \frac{-z + \sqrt{z^{2} + \delta^{2} r^{2}}}{\ell - z + \sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right] \left\{ -\frac{\ell - z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \frac{\ell - z}{\sqrt{z^{2} + \delta^{2} r^{2}}} + \ell n \left[ \frac{-z + \sqrt{z^{2} + \delta^{2} r^{2}}}{\ell - z + \sqrt{(\ell - z)^{2} + \delta^{2} r^{2}}} \right] \right\} - \frac{\ell - z}{\ell - z}$$

$$\frac{1}{4} (R^2)''' \left\{ \frac{z^2}{\sqrt{z^2 + \delta^2 r^2}} - \frac{(\ell - z)^2}{\sqrt{(\ell - z)^2 + \delta^2 r^2}} + 2\sqrt{(\ell - z)^2 + \delta^2 r^2} - 2\sqrt{z^2 + \delta^2 r^2} \right\} + \dots$$

Equation (21) can be rewritten in terms of the angles  $\alpha$  and  $\beta$  by noting that

$$V_{\infty}^{(x)} = V_{\infty} \sin \beta$$

$$V_{\infty}^{(y)} = V_{\infty} \sin \alpha \cos \beta$$

$$V_{\infty}^{(z)} = V_{\infty} \cos \alpha \cos \beta$$
(23)

and, thus,

$$C_{p} = \cos^{2}\alpha\cos^{2}\beta[-f-(R')^{2}] + \sin^{2}\beta[1-4\sin^{2}\theta] + \sin^{2}\alpha\cos^{2}\beta[1-4\cos^{2}\theta] +$$

$$\cos\alpha\sin^{2}\beta[-2R'\cos\theta] + \sin^{2}\alpha\cos^{2}\beta[-2R'\sin\theta] +$$

$$\sin^{2}\alpha\cos\beta[4\sin\theta\cos\theta]$$
(24)

where f and R' are evaluated on the body surface, i.e., r = R(z).

### 2.5 Angular and Static Pressure Sensitivity

The flow angularity is normally determined by differencing the measured pressures between the side and top and bottom parts, see Figure 1 for instance. Since these pressure ports are at the same z and R locations, the pressure difference is generated by subtracting  $C_p$  values at different  $\theta$  locations and

$$\Delta C_{p} = -4\sin^{2}\beta(\sin^{2}\theta_{2} - \sin^{2}\theta_{1}) - 4\sin^{2}\alpha\cos^{2}\beta(\cos^{2}\theta_{2} - \cos^{2}\theta_{1}) -$$

$$2R'\cos\alpha\sin^{2}\beta(\cos\theta_{2} - \cos\theta_{1}) - 2R'\sin^{2}\alpha\cos^{2}\beta(\sin\theta_{2} - \sin\theta_{1}) +$$

$$4\sin^{2}\alpha\cos\beta(\sin\theta_{2}\cos\theta_{2} - \sin\theta_{1}\cos\theta_{1})$$
(25)

The sensitivity to changes in flow angle is defined as  $\partial\Delta C_p/\partial\alpha$  or  $\partial\Delta C_p/\partial\beta$  . The former can be written as

$$\frac{\partial \Lambda C}{\partial \alpha} = -4\sin 2\alpha \cos^2 \beta (\cos^2 \theta_2 - \cos^2 \theta_1) + 2R'\sin \alpha \sin 2\beta (\cos \theta_2 - \cos \theta_1) - 4R'\cos 2\alpha \cos^2 \beta (\sin \theta_2 - \sin \theta_1) + 8\cos 2\alpha \cos \beta (\sin \theta_2 \cos \theta_2 - \sin \theta_1 \cos \theta_1)$$
(26)

This expression can be considerably simplified by choosing  $\theta_1$  and  $\theta_2$  as  $90^\circ$  and  $270^\circ$  respectively. Equation (26) then becomes

$$\frac{\partial \Delta C_{p}}{\partial \alpha} = 8R'\cos 2\alpha \cos^{2}\beta \tag{27}$$

Note that the sensitivity to flow direction in one plane depends to some extent on the flow angle in the other direction.

 $\partial \Delta c_p / \partial \beta$  can be determined in a similar manner with  $\theta_1$  and  $\theta_2$  taking the values of 0 and 180. This yields

$$\frac{\partial \Delta C_{\mathbf{p}}}{\partial \beta} = 8R' \cos \alpha \cos 2\beta \tag{28}$$

Note that the two expressions, i.e.,  $\partial \Delta C_p/\partial \alpha$  and  $\partial \Delta C_p/\partial \beta$ , are not symmetric in terms of  $\alpha$  and  $\beta$  even though equation (21) is symmetric in terms of  $V_{\infty}^{(x)}$ ,  $V_{\infty}^{(y)}$  and  $V_{\infty}^{(z)}$ . This is due to the definition of  $\alpha$  and  $\beta$ .  $\alpha$  is referenced to x, y and z while  $\beta$  is referenced to a vector rotated through the angle  $\alpha$ . If both  $\alpha$  and  $\beta$  are referenced to the x, y and z axes, then equations (27) and (28) - although somewhat more complex - are symmetric with regard to flow angle.

Equation (27) is plotted in Figure 3. It is quite apparent from both the mathematical relation and the figure that the probe sensitivity - regardless of shape - depends on  $\alpha$  and  $\beta$ . A 10% reduction in sensitivity occurs for  $\alpha$  and  $\beta$  of 10°. Note that  $\partial \Delta C_p / \partial \alpha$  is the same for both positive and negative values of  $\alpha$  and  $\beta$ .

The averaged pressure coefficient can be used to determine the actual flow field static pressure, i.e.,  $p_{\infty}$ .  $C_{p}$  is evaluated at a number of theta values, normally  $0^{\circ}$ ,  $90^{\circ}$ ,  $180^{\circ}$  and  $270^{\circ}$ , the results summed and divided by the number of points. Mathematically, this becomes

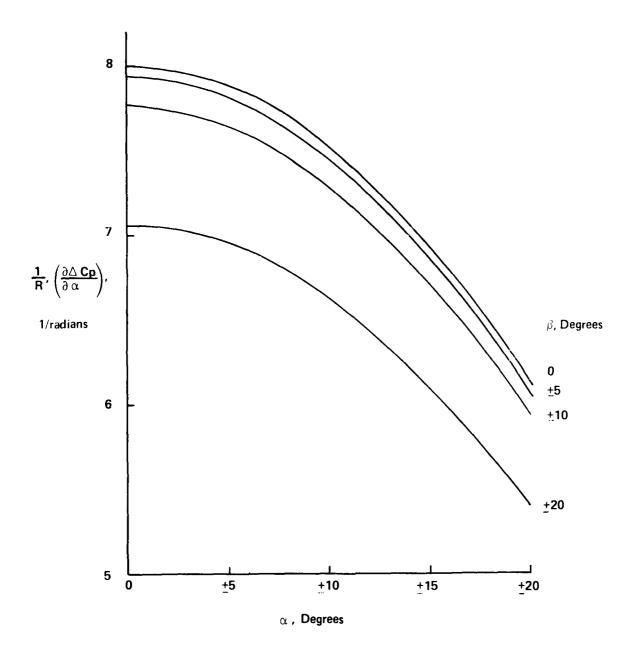


Figure 3. Probe Angular Sensitivity as a Function of  $\alpha$  and  $\beta$ 

$$\langle C_{p} \rangle = \cos^{2}\alpha\cos^{2}\beta[-f-(R')^{2}] + \sin^{2}\beta\left(1 - \sum_{i=2}^{5}\sin^{2}\theta_{i}\right) +$$

$$\sin^{2}\alpha\cos^{2}\beta\left(1 - \sum_{i=2}^{5}\cos^{2}\theta_{i}\right) - \frac{1}{2}R'\cos\alpha\sin^{2}\beta\sum_{i=2}^{5}\cos\theta_{i} -$$

$$\frac{1}{2}R'\sin^{2}\alpha\cos^{2}\beta\sum_{i=2}^{5}\sin\theta_{i} + \sin^{2}\alpha\cos\beta\sum_{i=2}^{5}\sin\theta_{i}\cos\theta_{i}$$
(29)

When  $\theta_i$  is chosen as  $0^\circ$ ,  $90^\circ$ ,  $180^\circ$  and  $270^\circ$ , the above relation becomes

$$\langle C_{p} \rangle = \cos^{2}\alpha\cos^{2}\beta[-f-(R')^{2}] - \sin^{2}\beta - \sin^{2}\alpha\cos^{2}\beta$$
 (30)

which is approximately parabolic with regard to  $\alpha$  and  $\beta$ . Equation (30) also has the same value for both positive and negative  $\alpha$  and  $\beta$ 's.

The analysis is restricted to small perturbation velocities and, thus, a total pressure coefficient cannot be directly derived. A quasi-total pressure can be formulated by integrating the pressure over the body surface area and resolving this force into x, y and z components. An axial pressure can be generated by dividing the z component by the probe cross-sectional area. This has the form of a total pressure but is less in value since the flow is never stagnated - except at z = 0 where the body cross-sectional area is also zero. The functional form of this relation is

$$C_{p_{z}} = \frac{p_{z}^{-p_{\infty}}}{q_{\infty}} = \frac{\cos^{2}\alpha\cos^{2}\beta}{R_{\ell}^{2}} \int_{0}^{\ell} (R^{2})'[-f-(R')^{2}]dz - \sin^{2}\beta - \sin^{2}\alpha\cos^{2}\beta$$
 (31)

where  $\ell$  denotes the length of the body in the z-direction over which the integration is to be performed. The coefficient again decreases in an approximately parabolic manner with  $\alpha$  and  $\beta$ .

The analytical relationships of this section are compared to measured probe characteristics in Section 4. The experimental data in conjunction with the theoretical results is used to demonstrate the general characteristics of probes in Section 6.

#### SECTION 111

#### EXPERIMENTAL PROGRAM

### 3.1 Introduction

While the relationships of Section 2 are valuable for characterization of probe behavior, they are not capable of replacing individual probe catibrations. This is due to the limitations of the derivation itself, i.e., inviscid flow and stender body assumptions, as well as the manufacturing irregularities in the probe, i.e., asymmetric construction, misalignment of pressure ports, static ports not normal to probe surface, etc. Regardless of the accuracy of the theoretical derivations, the latter effects may necessitate individual probe calibrations - particularly for small probes. In the present context, the data generated in the calibration can be used to assess the reliability of the mathematical model as well as furnish the angular and Mach number characteristics of the probe which will, in turn, be used in the experimental study of compressor performance, reference 20. The details of the probe calibration are discussed in the following sections.

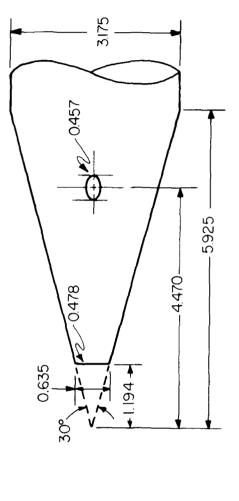
### 3.2 Experimental Apparatus

The probe employed in the calibration process consisted of truncated cone with four side pressure taps nominally normal contract. The maximum conic diameter is 3.175mm (0.1250 in. w. or total pressure port having an internal diameter of 0.055 inh and the side ports having internal diameters of 0.457mm (0.016 in A photograph and a dimensioned sketch of the probe are shown in Figure 4.

The probe was calibrated using a DISA 55D90 calibration system, reterence 27. This system consists of a pressure controller, stagnation chamber and nozzle asembly and a three-axis probe positioning system. The system elements are shown in Figures 5 and 6.

The flow and/or pressure controller utilizes a three-stage pressure regulator producing an extremely stable flow which is supplied to the stagnation chamber in the nozzle assembly. The stagnation chamber contains a honeycomb flow straightner and four turbulence damping screens. This generates a very low turbulence level flow field. The unit is fitted with





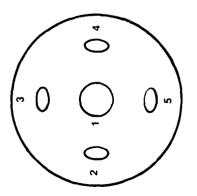
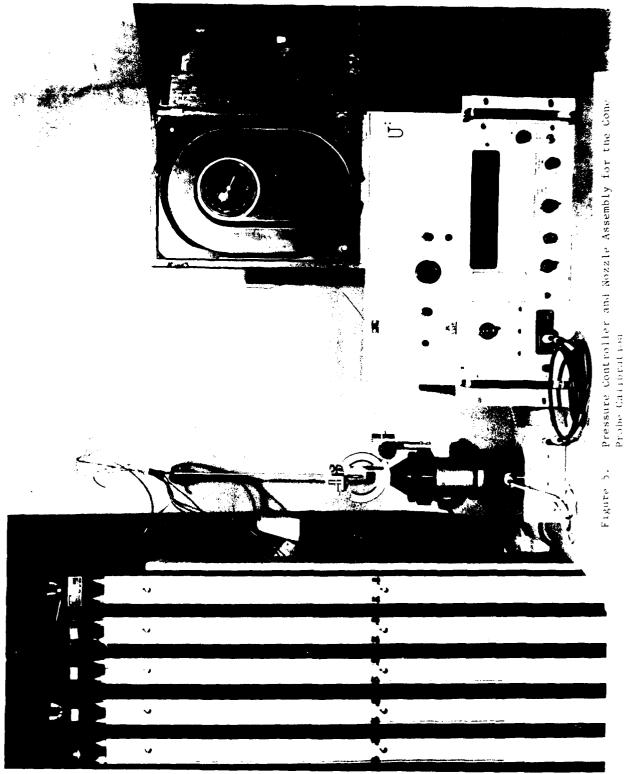


Figure 4.  $30^{\rm O}$  Included Angle, Truncated Conical Probe (all dimensions in mm)



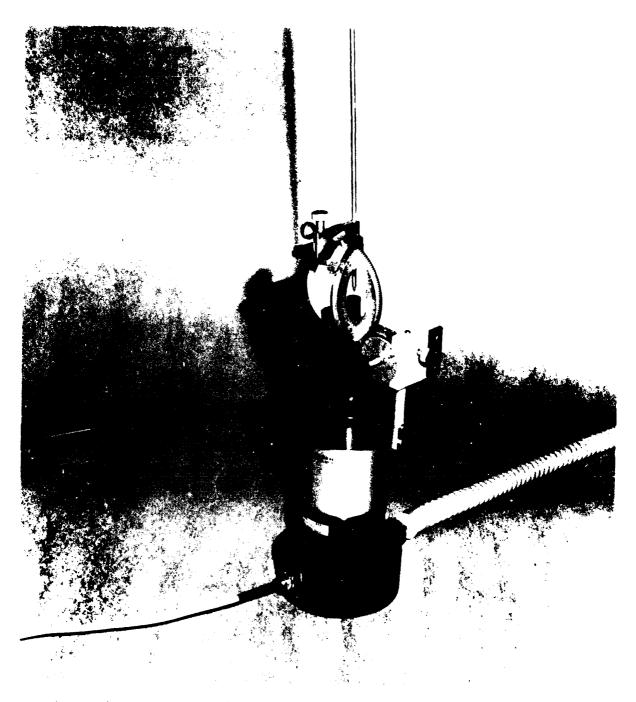


Figure 6. Stagnation Chamber, Nozzle and Probe Positioning Assembly

four interchangeable converging nozzles. The velocity can be varied from 0.5 m/sec (1.6 ft/sec) to sonic conditions by interchanging nozzles and varying the stagnation chamber pressure levels. The pressure controller is nominally supplied with air at an absolute pressure of 144.8 x  $10^8$  kgr/m<sup>2</sup> (100  $1b_e/in^2$ ).

The nozzle chosen for the experimentation has a discharge area of 60mm<sup>2</sup> (0.093 in<sup>2</sup>). Probe blockage corrections - discussed in Section 3.4 - indicated that this nozzle could be used for all Mach numbers investigated. The fairly large mass flow rates at the higher Mach numbers exceeded the capacity of the DISA pressure controller and it was replaced with two series installed, control valves for the high Mach number tests. The flow remained stable but controllability was sacrificed.

The probe is mounted in the potential core of the free jet discharged from the nozzle. The probe positioning mechanism is mounted on a vertical column which is permanently fixed to the main nozzle unit. The nozzles can be interchanged without removing the probe. The probe can be rotated in both the angle-of-attach,  $\alpha$ , and side-slip,  $\beta$ , planes -  $\alpha$  can be measured to an accuracy of  $\pm$  0.1° while the  $\beta$  resolution is limited to  $\pm$  0.5°. The probe can also be positioned both axially and in roll. All four of these positioning freedoms are shown in Figure 6. The probe tip is nominally located one nozzle radius downstream of the nozzle exit plane. The size of the probe relative to the nozzle limits  $\alpha$  and  $\beta$  to

$$-20^{\circ} \leq \alpha \leq 20^{\circ}$$

$$0 \leq \beta \leq 20^{\circ}$$
(32)

### 3.3 Measurement Methods

The primary objective of the calibration was to determine the angular,  $\Delta C_{p\alpha}$  and  $\Delta C_{p\beta}$ , averaged,  $^{<}C_{p}$  >, and total,  $^{C}_{p\tau}$ , pressure coefficients. These are easily generated from the measured probe pressures and the nozzle total and static pressures. Since the parameters are all - more or less - Mach number and Reynolds number dependent, the gas temperature and relative humidity must also be measured.

The angular coefficients are defined as

$$\Delta C_{\mathbf{p}_{\alpha}} = \frac{\mathbf{p}_{2} - \mathbf{p}_{4}}{\mathbf{p}_{+} - \mathbf{p}_{\infty}} \tag{33}$$

$$\Delta C_{p_{\beta}} = \frac{p_3 - p_5}{p_t - p_{\infty}} \tag{34}$$

which correspond to the definitions of Section 2. The averaged pressure coefficient can be defined as

$$\langle C_p \rangle = \frac{\langle p \rangle - p_{\infty}}{p_t - p_{\infty}} \tag{35}$$

where  $\langle p \rangle = \frac{1}{4}(p_2 + p_3 + p_4 + p_5)$ . The total pressure coefficient follows the definition in equation (31) and

$$C_{p_{t}} = \frac{p_{1} - p_{\infty}}{p_{t} - p_{\infty}} \tag{36}$$

Alternate formulations are certainly possible, i.e., replace  $p_t^-p_\infty$  with  $p_1^-p_\infty^-$  in equations (33), (34) and (35) and redefine  $C_{p_t}$  as  $(p_t^-p_1)/p_1^-<p^>)$ , but the above most closely follow the theory and should exhibit more nearly universal behavior.

In any event, all coefficients represent pressure differences and one is tempted to measure these directly. Direct measurement of the differences is, however, complicated by the requirement to average the side port pressures. When all the necessary pneumatic connections are formulated, this task becomes formidable. Furthermore, the frequency response - which is already of order of minutes due to the small tube diameters - is further degraded as a result of the tubing, connectors and fittings required in the differencing and averaging processes. Note also that the pneumatic connections are designed for a specific series of coefficients. This considerably limits the computation of different forms of coefficients in the data reduction process.

As a result of these considerations, the pressures  $p_1$ ,  $p_2$ ,  $p_3$ ,  $p_4$ ,  $p_5$ , and  $p_t$  were measured independently using a bank of inclined water manometers. The manometers could be read to 1.270mm (0.05 in) of water in the vertical position. With the manometer bank inclined at  $10^{\circ}$ , the

maximum pressure resolution then becomes 0.221mm (0.009 in) of water. At a Mach number of 0.2, the maximum angular resolution - as determined from pressure measurements - is approximately 0.02° for a 30° conical probe. This is well in excess of the angular measurement accuracy of 0.1° and, thus, the pressure measurement accuracy as afforded by the inclined water manometers is sufficient. In terms of pressure differences, the angular probe sensitivity scales with the dynamic head and, thus, pressure measurement resolution can be increased with increasing Mach numbers while maintaining the same pressure based, angular resolution. In the test program, the manometer inclination was increased at the higher Mach numbers which reduced the pressure measurement resolution but maintained the angular resolution at its low Mach number value.

The gas total temperature was measured in the nozzle unit stagnation chamber prior to the flow conditioning devices with a bimetallic element. Air temperatures nominally varied from 20 to  $30^{\circ}$ C. The relative humidity of the supply air remained below 5% as measured by an Environmental Tektronics Corporation Psychor-dial Model CP-147 psychrometer.

As previously noted, the probe can be rotated along its longitudinal axis. It is essential that the probe side ports be aligned with the  $\alpha$  and  $\beta$  axes respectively. This alignment was done by rotating the probe until the  $p_3$ - $p_5$  pressure differential was symmetric throughout the usable range. This proved to be a time consuming process because the probe was extremely sensitive to even the slightest rotation and the manometer response was very slow, i.e., approximately five minutes were required for the manometers to come to equilibrium.

### 3.4 Aerodynamic Considerations

The use of a free jet in the calibration process presumes that the jet velocity in the vicinity of the probe is uniform and equal to the value of the nozzle exit plane. Two major factors can influence the above assumptions. First, the presence of the probe in the jet creates "blockage" which causes the jet to spread and can result in a reduction of velocity. In a closed wind tunnel, probe and/or model blockage results in velocity increases. Secondly, the jet potential core decreases with downstream distance yielding a spatially non-uniform flow field.

If the free jet is assumed to be similar to an open jet wind tunnel, then probe blockage effects can be computed using the wind tunnel techniques. Following the methods of reference 28, a velocity decrease, i.e.,  $\Delta V_{\infty}/V_{\infty}$ , of approximately 1.7% will occur for Mach number of 0.2 increasing to 3.1% at Mach numbers of 0.6. The results are based on a jet nozzle diameter of 8.740mm (0.344 in) and a probe diameter of 3.175mm (0.125 in). The blockage increases rapidly with reduction in nozzle size reaching a value of 12.2% for a nozzle diameter of 5.528mm (0.218 in) at  $M_{\infty} = 0.6$ . In general, the blockage obtained with the larger nozzle,  $d_{\rm n} = 8.740$ mm, is satisfactory; smaller nozzles, however, should not be used.

The decrease in jet potential core width can result in an apparent spatially non-uniform flowfield if the probe is not positioned within the potential core – a potential problem at large values of  $\alpha$  and  $\beta$ . The jet potential core decreases at the angle  $\theta_j$  which is approximately  $6-7^\circ$ , reference 29. This value implies a potential core having a diameter of about 77% of the nozzle diameter  $d_n$  downstream of the nozzle. Data from reference 30 indicates a potential core diameter of about 0.85  $d_n$  at the same axial location. Consequently,  $6-7^\circ$  may slightly overestimate the core decrease but should yield conservative results. The probe in the aligned and maximum displacement positions is shown in Figure 7. It is well within the jet potential core even in the latter case.

The nozzle of diameter 8.740mm (0.344 in) coupled with the probe of diameter 3.175mm (0.125 in) yield acceptably low blockage values at  $\alpha$  and  $\beta$  values of up to  $20^{\circ}$  Furthermore, the probe tip and side ports remain within the potential jet core at the same angles.

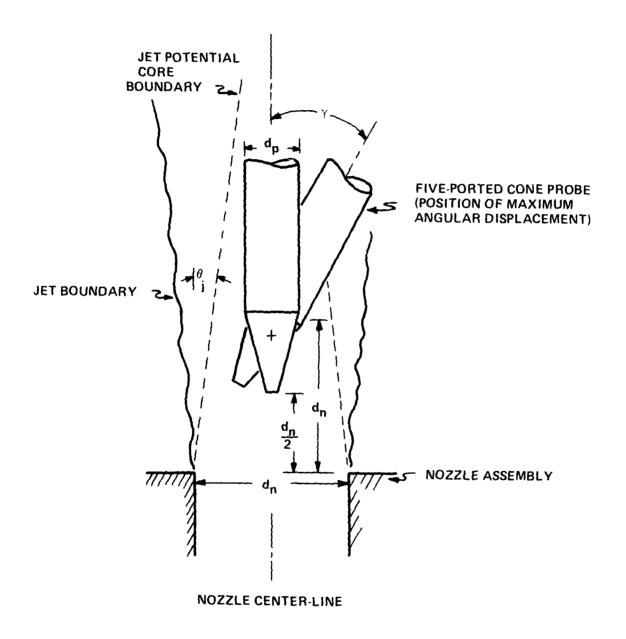


Figure 7. Schematic Diagram of the Calibration Jet and the Five-ported, Conical Probe

### SECTION IV

### EXPERIMENTAL RESULTS

#### 4.1 Introduction

The experimental data was acquired using the apparatus and measurement techniques described in the previous section. Probe calibration data was taken at three Mach numbers and 91 angular positions per Mach number, i.e.,  $\beta$  = 0, 2.5, 5.0, 7.5, 10, 15, and 20, and  $\alpha$  = -20, -15, -10, -7.5, -5.0, -2.5. 0, 2.5, 5.0, 7.5, 10, 15, 20 for each  $\beta$  value;  $M_{\infty}$  = 0.2, 0.4 0.6. In addition, <C  $_p$  > was evaluated at 16 Mach numbers ranging from 0.05 to 0.60. Data reduction and plotting was automated using the AF Academy computer system. The data reduction techniques and the data itself are discussed in the following sections.

#### 4.2 Data Reduction Methods

The angular, total and static pressure coefficients were computed as defined in Section 3.3. The velocity, Mach number and Reynolds numbers were computed using the algorithms of reference 26. Since the nozzle assembly discharges to atmospheric pressure, the Reynolds number and Mach number are uniquely related with Reynolds numbers of 10505, 23896, and 37853 based on probe diameter, corresponding to Mach numbers of 0.2, 0.4 and 0.6.

The probe Reynolds numbers encountered in the compressor tests will range from 29700 to 61052. This exceeds the calibration values at the equivalent Mach number; however, the probe boundary layers are undoubtedly turbulent in either case and, thus, the difference in Reynolds numbers should not influence the calibration functions.

### 4.3 Experimental Data

The experimental results are presented in Tables 1, 2, 3 and 4 and Figures 8 through 19. Table 1 and Figures 8 through 11 summarize the data for a Mach number of approximately 0.2, with Table 2 and Figures 12 through 15 corresponding to M  $_{0}$   $^{2}$  0.4, and Table 3 and Figures 16 through 19 dealing with data of M  $_{\infty}$   $^{2}$  0.6. Table 4 and Figure 20 contains the results of the fixed position, i.e.,  $\alpha$  =  $\beta$  = 0, variable Mach number runs, i.e.,  $0.05 \le M_{\infty} \le 0.6$ .

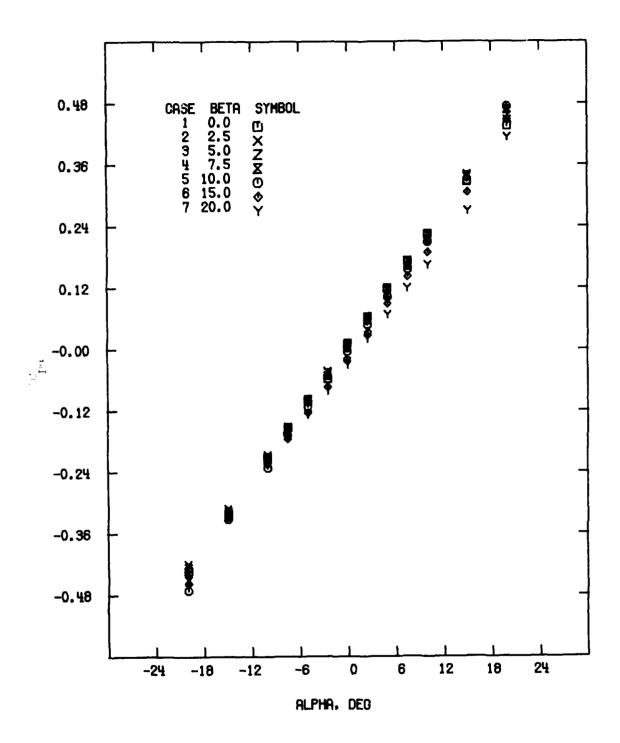


Figure 8.  $\Delta C_{\mbox{$p_{\alpha}$}}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $\mbox{$M_{\infty}$} \cong 0.2$ 

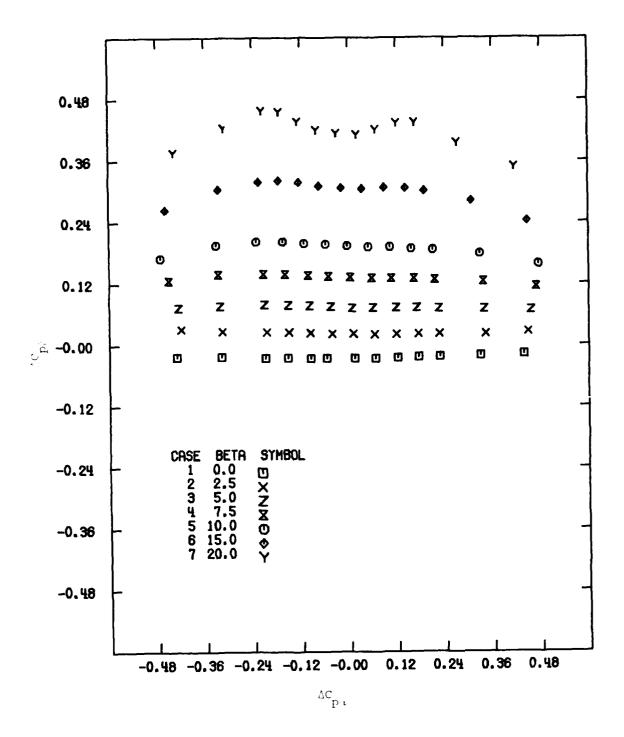


Figure 9.  $\begin{array}{ccc} \Delta C_{p_{C\!\!\!/}} & \text{versus } \Delta C_{p_{\beta}} & \text{for the Five-ported, Conical Probe} \\ M_{\infty} & \cong & 0.2 \end{array}$ 

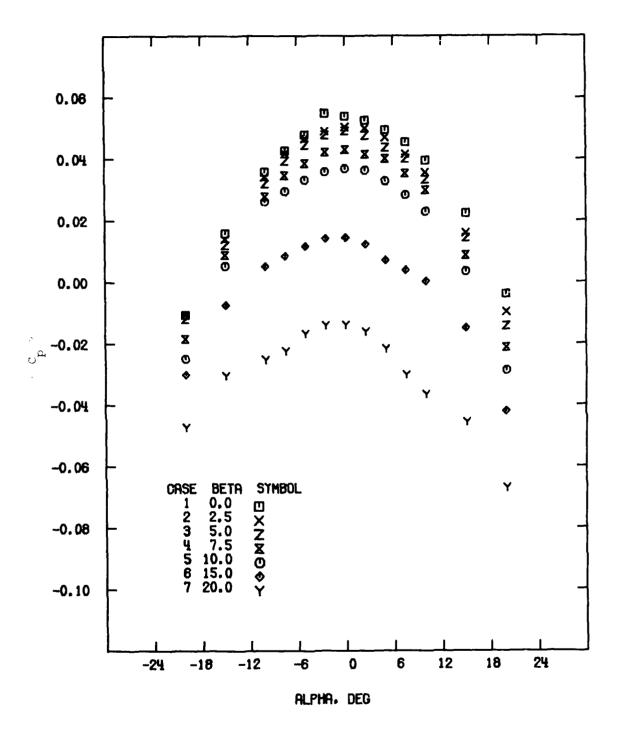


Figure 10.  $^{< C}p^{>}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $\text{M}_{\infty}$   $^{\simeq}$  0.2

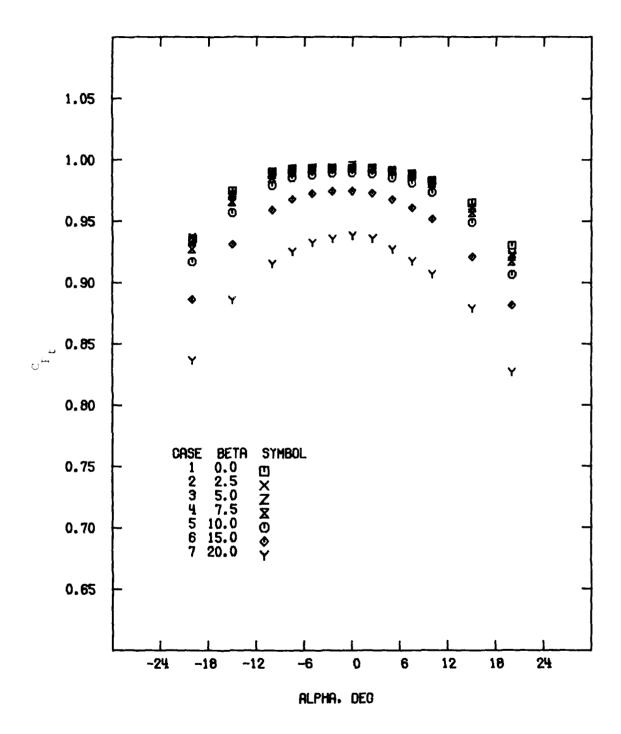


Figure 11.  $C_{\mbox{\scriptsize p}}_{\mbox{\scriptsize t}}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $M_{\mbox{\scriptsize en}}^{} \simeq 0.2$ 

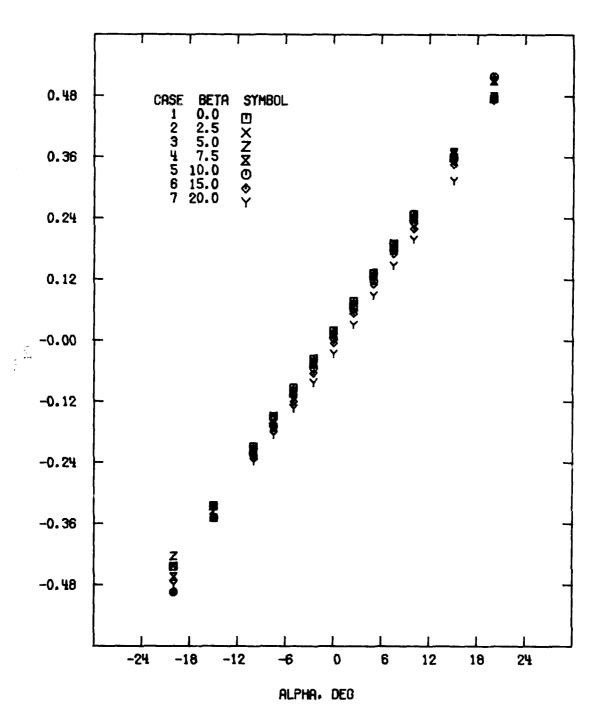


Figure 12.  $\Delta C_{\mbox{$p_{\alpha}$}}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $M_{\mbox{$m$}} \simeq 0.4$ 

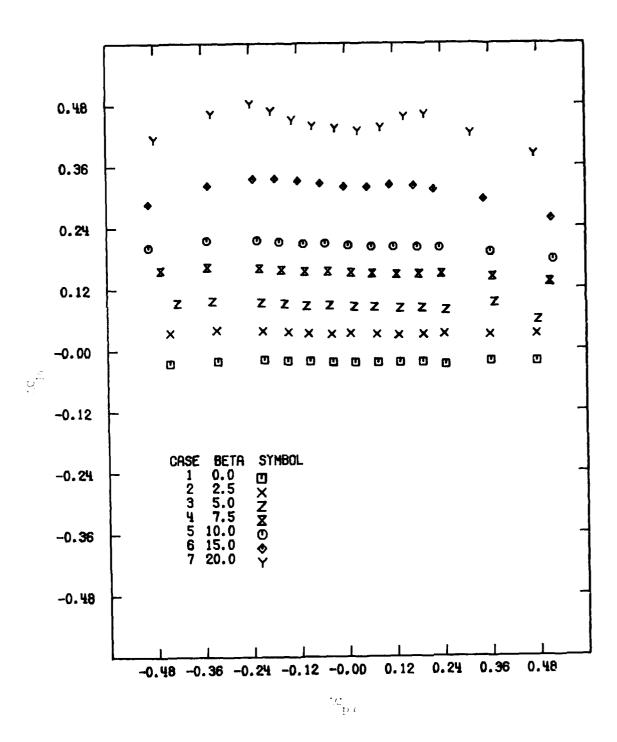


Figure 13.  $\Delta C_{p_{\alpha}}$  versus  $\Delta C_{p_{\beta}}$  for the Five-ported, Conical Probe,  $M_{\infty}\stackrel{\sim}{=} 0.4$ 

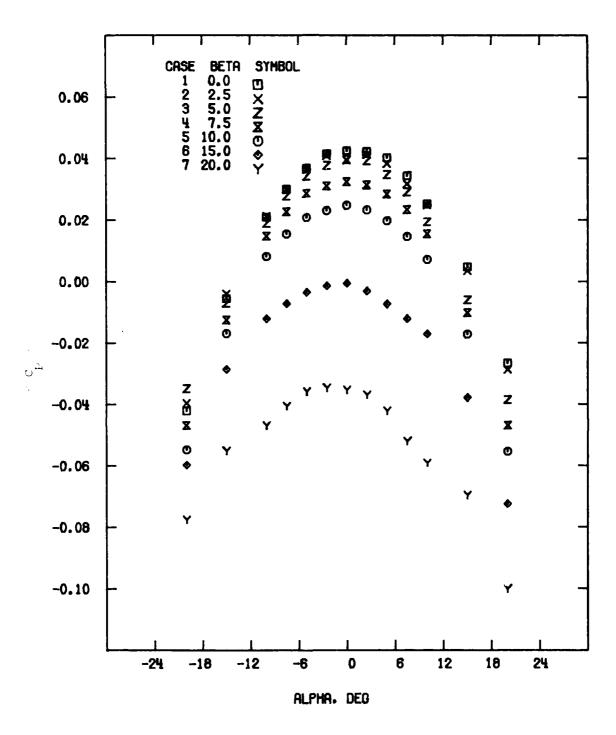


Figure 14.  $^{<}C_{p}^{>}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $^{M}_{\infty}$   $^{\simeq}$  0.4

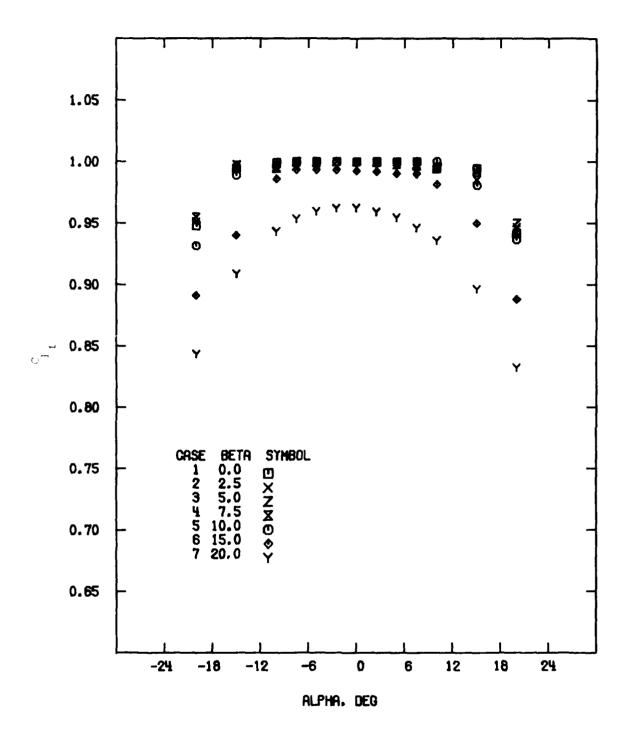


Figure 15.  $C_{\mbox{\scriptsize p}}_{t}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $M_{co}^{}\simeq 0.4$ 

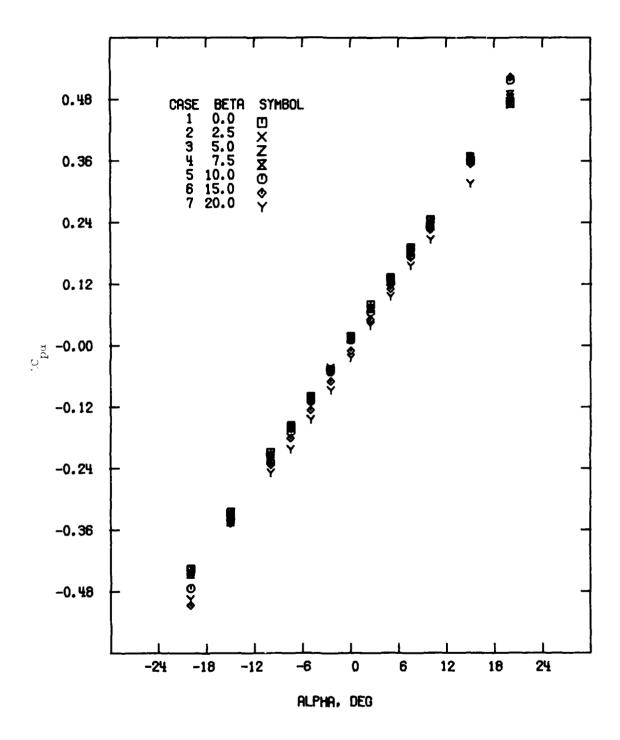


Figure 16.  $\Delta C_{\mbox{$p_{\alpha}$}}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $\mbox{$M_{\infty}$} \stackrel{?}{\simeq} 0.6$ 

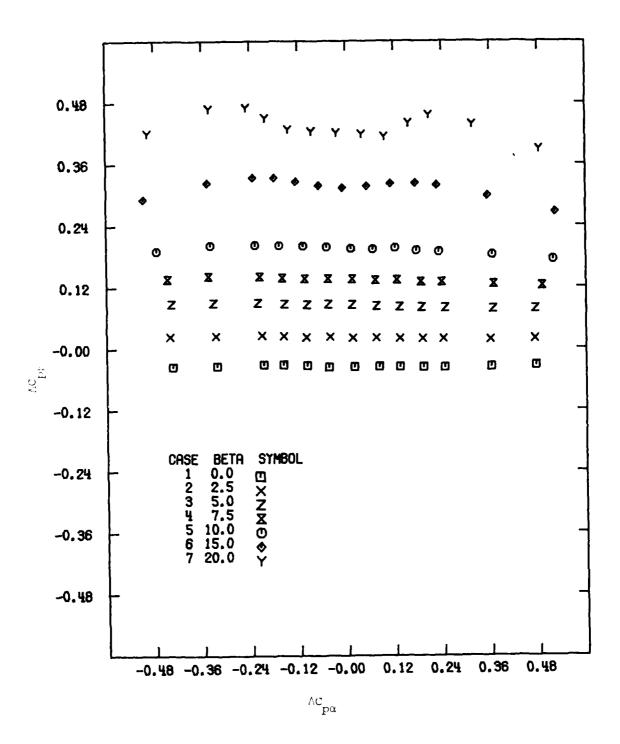


Figure 17.  $\Delta C_{\begin{subarray}{c} D_{C}\\ M_{\infty} \end{subarray}} \begin{subarray}{c} \Delta C_{\begin{subarray}{c} D_{\beta} \end{subarray}} \begin{subarray}{c} for the Five-ported, Conical Probe, M_{\infty} \end{subarray}$ 

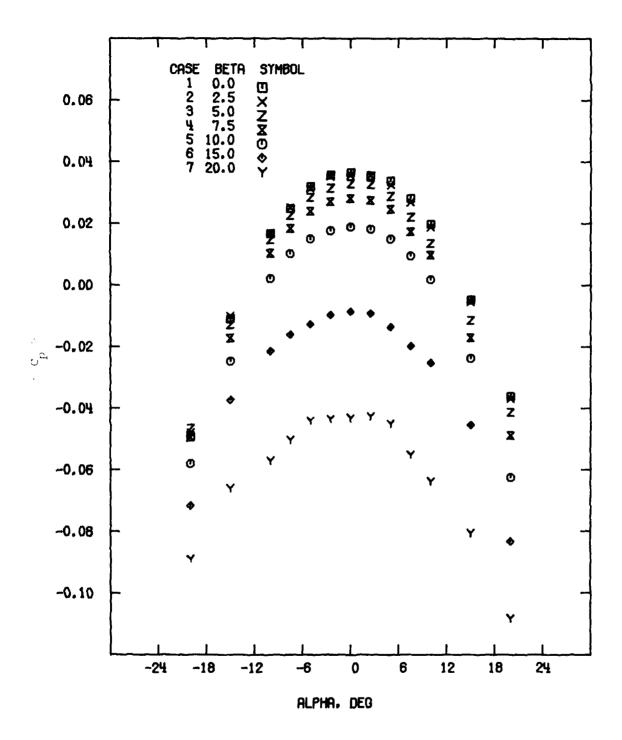


Figure 18.  $<\!\!c_p\!\!>$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $\underset{\infty}{\text{M}}\simeq 0.6$ 

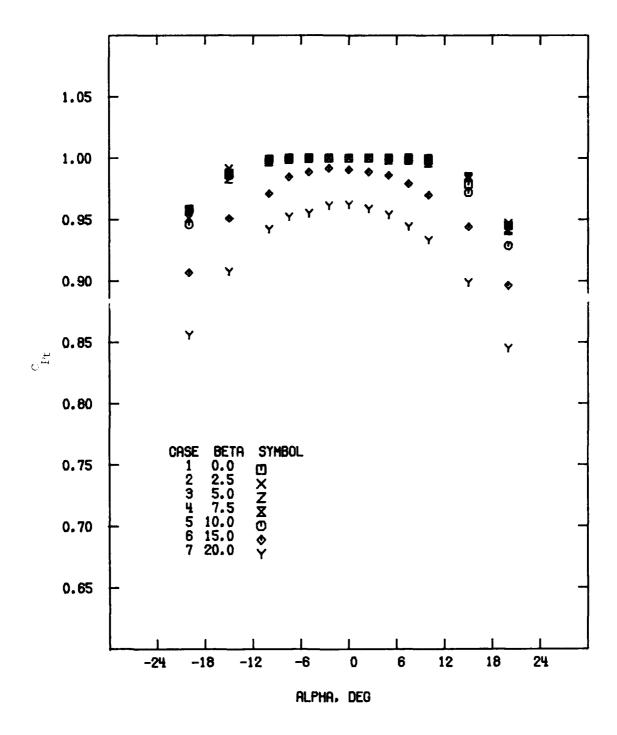


Figure 19.  $C_{p,t}$  versus  $\alpha$  and  $\beta$  for the Five-ported, Conical Probe,  $M_{cr}^{+} \cong 0.6$ 

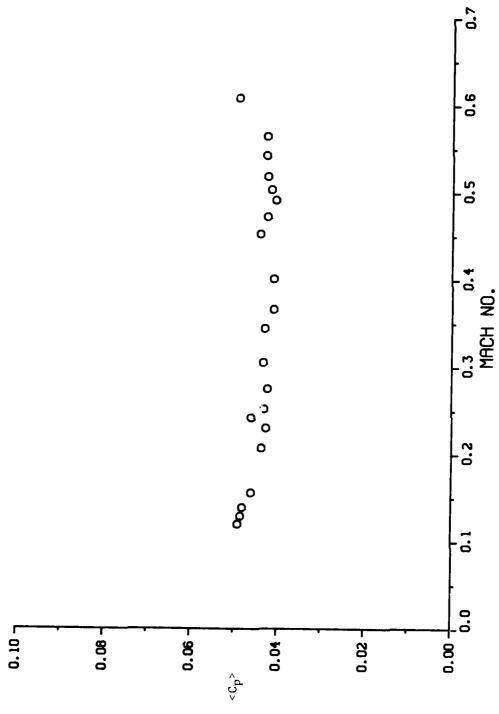


FIGURE 20.  $< C_p > VERSUS \ M_{\infty}$  FOR THE FIVE-PORTED, CONICAL PROBE,  $\alpha = \beta = 0$ 

The parameters of Section 2,  $^{\Lambda C}p_{\alpha}$ ,  $^{\Lambda C}p_{\beta}$ ,  $^{< C}p^{>}$  and  $^{C}p_{t}$ , are plotted in the three groups of figures. Figures 8, 12 and 16 depict the variation of  $^{\Lambda C}p_{\alpha}$  with  $^{\alpha}$ ,  $^{\beta}$  and Mach number. Figures 9, 13 and 17 consist of crossplots of  $^{\Lambda C}p_{\alpha}$  versus  $^{\Lambda C}p_{\beta}$ .  $^{< C}p^{>}$  is plotted in Figures 10, 14 and 18 for the three Mach numbers with  $^{C}p_{t}$  plotted in Figures 11, 15 and 19. Figure 20 shows the variability of  $^{< C}p^{>}$  with Mach number.

The probe performance generally confirms to the analytic relations of Section 2. From Figure 3, it can be concluded that  $\Delta C_{p_\alpha}$  and/or  $\Delta C_{p_\beta}$  should vary linearily with  $\alpha$  and for  $\beta$  over small angular ranges becoming nonlinear as the angles increase. This trend is shown in Figures 8, 9, 12, 13, 16 and 17. The decrease in angular response is particularly evident in Figures 9, 13 and 17 at the higher values of  $\alpha$  and  $\beta$ , i.e.,  $\Delta C_{p_\beta}$  tends to increase at a lesser rate as  $\alpha$  and  $\beta$  exceed about  $10^{\circ}$ .

 ${}^{<\!C_p>}$  and  ${}^{C_p}$  both vary predominately with  $\alpha^2$  and  $\beta^2$  as shown in equations (30) and (31), i.e.,

$$\langle C_{p} \rangle \simeq (1 - \alpha^{2} - \beta^{2}) [-f - (R')^{2}] - \beta^{2} - \alpha^{2}$$

$$C_{p_{z}} \simeq \frac{(1 - \alpha^{2} - \beta^{2})}{R_{\chi}^{2}} \int_{\Omega}^{\ell} (R^{2}) [-f - (R')^{2}] dz - \beta^{2} - \alpha^{2}$$
(37)

where higher order terms have been neglected.

According to the slender body analysis of Section 2, only the function f is Mach number dependent and, thus,  $\Delta C_{p_{\alpha}}$  and  $\Delta C_{p_{\beta}}$  should be independent of Mach number while  ${}^{<}C_{p}{}^{>}$  and  $C_{p_{z}}$  are functions of Mach number. This result is more--or less--confirmed experimentally. The angularity coefficients are much less Mach number dependent than the averaged static pressure or total pressure coefficients. This can be seen by comparing Figures 8 through 11 with Figures 12 through 15 or Figures 16 through 19.

The Mach number dependence of  ${}^{<}C_p{}^{>}$  is not particularly pronounced in the subsonic flow regions. Figure 20 and Table 4 show only a modest variation in this parameter as the Mach number is increased from 0.12 to 0.61.

# 4.4 Summary of Experimental Results

The angularity coefficients, i.e., flow direction coefficients, and static and total pressure coefficients behave, functionally, in a manner

consistent with equations (25), (30) and (31).  $\Delta C_{p_{\alpha}}$  and  $\Delta C_{p_{\beta}}$  vary linearly with  $\alpha$  and  $\beta$  for small and moderate angles while  $< C_p >$  and  $C_{p_t}$  varying with  $\alpha^2$  and  $\beta^2$ . Both  $\Delta C_{p_{\alpha}}$  and  $\Delta C_{p_{\beta}}$  are independent of Mach number while  $< C_p >$  and  $C_{p_t}$  are Mach number dependent. The data scatter is well within acceptable bounds for angles up to  $10^{\circ}$  and increases somewhat at the larger angles. The behavior at the larger angles may be due to flow separation on the probe itself or flow blockage effects as discussed in Section 3.4.

### SECTION V

### COMPARISON OF THEORETICAL AND EXPERIMENTAL RESULTS

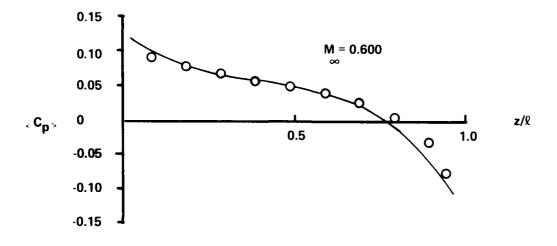
## 5.1 Averaged Pressure Coefficient

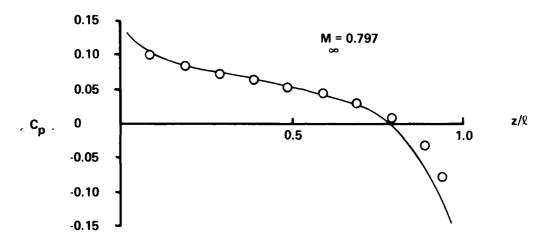
The subsonic, transonic and supersonic flow field about a cone has been measured by many investigators. Some typical experimental results, reference 29, are compared with equation (30) in Figure 21. Note that the conditions correspond to an angle of attack and side-slip angle of  $0^{\circ}$ . The mathematical model of Section 2 is limited to subsonic Mach numbers, i.e., the Mach number must be less than 1 on all points of the conic surface. This corresponds to a freestream Mach number,  $M_{\infty}$ , of approximately 0.9 and, thus, the experimental theoretical comparison has been limited to this value. The analytic predictions correspond closely to the measured values over about 75-80% of the cone length. The calculated <C $_p>$  values are less than the measured points over the latter portions of the cone,  $0.75 \le z/\ell \le 1.00$ , with the deviation increasing as the Mach numbers approach one.

The cone of reference 29 has an included angle of 6.983°, a length of 139.7mm (5.50 in) and a maximum diameter of 34.214mm (1.347 in). The model is sufficiently large so that the static pressure ports can be assumed to be normal to the cone surface. The tests were carried out in two separate wind tunnels, i.e., NASA Ames 2 by 2 foot and 14 by 14 foot transonic wind tunnels, and both sets of data agree to within the accuracy of the measurements. As a consequence, there is every reason to believe that the data is accurate. The disparity between the measured and calculated results over the aft-portion of the cone must then be due to a failure of the theory itself.

The calculated pressure coefficients for the cone probe of Section 4 are shown in Figures 22, 23 and 24. Figure 22 depicts the variation of the averaged pressure coefficient as a function of position,  $z/\xi$ , and Mach number. The section diagram shows the location of the static ports and the point of cone truncation. Figure 23 is a plot of  $C_p$  as a function of Mach number while Figure 24 shows  $C_p$  as a function of  $\alpha$  and  $\beta$ .

While the general trends of the data are reproduced by the analysis of Section 2, the overall levels are considerably less than the measured values. As noted in previous paragraphs, the mathematical model tends to





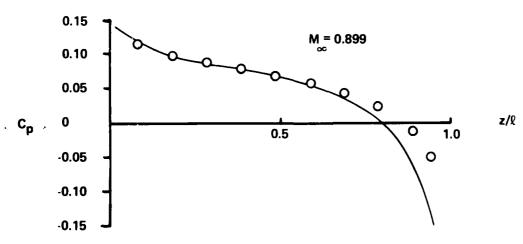
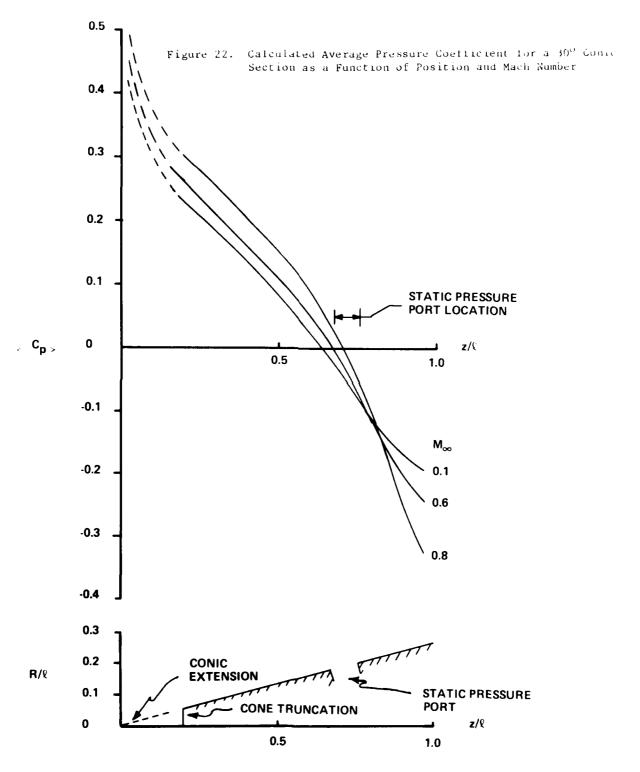


Figure 21. Comparison of Measured and Calculated Averaged Pressure Coefficients for a 70 Conic Section



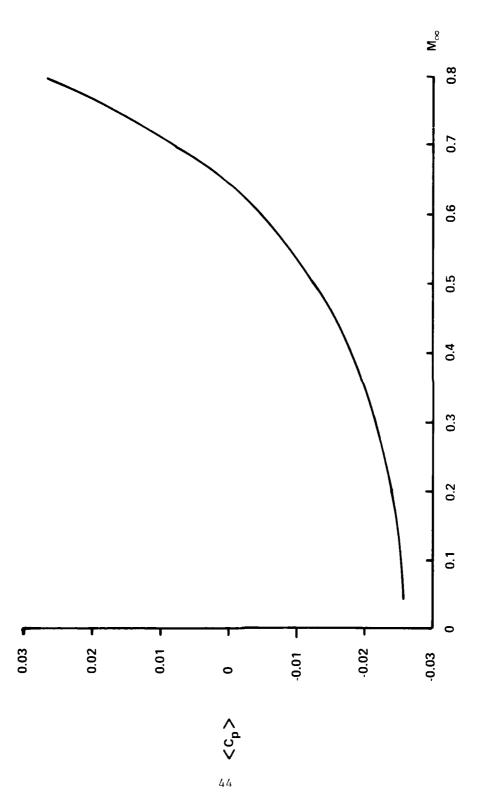


Figure 23. Calcatated Cone Probe Pressure Distribution as a Function of Mass Samber,  $\tau=|\nu|=0$  and  $z/\ell=0.68$ 

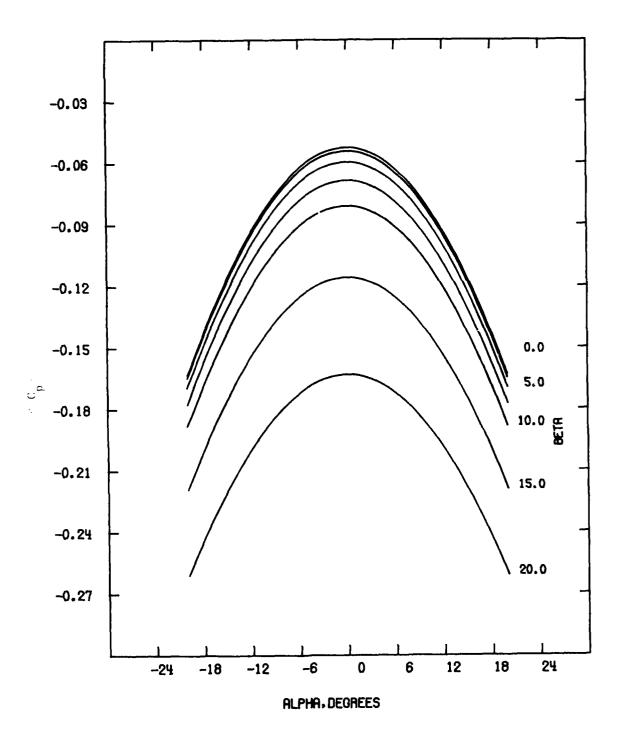


Figure 24. Averaged Pressure Coefficient for a 30° Cone Probe,  $M_{\alpha}=0.20$  and  $z/\ell=0.68$ 

underestimate the  ${}^{\circ}C_{p}^{-}$  values on the latter portion of the cone. Other potential sources of error are static pressure hole diameter and depth, references 30 and 31, hole geometry, reference 32, hole not normal to cone surface and turbulence level, reference 33. It was initially believed that the truncation of the cone might alter the measured static pressures. The low and variable Mach number tests of Section 4 were, however, repeated for a sharp-nosed cone with little or no change in the measured pressure coefficients. As a consequence, it was concluded that cone truncation - of the magnitude shown in Figure 22 - does not influence the static pressure measurements.

The magnitude of corrections for pressure tube geometry are of the order of the difference between the calculated and measured values if the static holes are slightly rounded, i.e., a correction of approximately 0.5-1% of the dynamic head for a corner radius of 0.114mm (0.005 in). This effect, coupled with the underestimate of Figure 21, are probably the main cause of the discrepancy between the calculated and measured values, e.g., Figures 20 and 23 and Figures 10 and 24.

The difference between the calculated and measured results again points out the need to calibrate individual probes, particularly the extremely small sensors used in turbine engine tests. It is unlikely that probes of the type and size discussed in Section 4 can be manufactured without some anamolous behavior.

# 5.2 Angular Pressure Coefficients

The angular pressure coefficient data of Section 4,  $\Delta C_{p\alpha}$  and  $\Delta C_{p\beta}$ , can be compared to the theoretical results of Section 2, equation (25). Equation (25) infers that  $\Delta C_{p\alpha}$  is proportional to the local surface gradient, dR/dz, the sin  $2\alpha$  and  $\cos^2\beta$ . As a consequence,  $\Delta C_{p\alpha}$  is approximately linear with  $\alpha$  for small angles of attach, is independent of Mach number and is only slightly dependent on  $\beta$  for small  $\beta$  values. Calculated values for  $\Delta C_{p\alpha}$  and  $\Delta C_{p\beta}$  as a function of  $\alpha$  and  $\beta$  are shown in Figure 25. These results are in general comparable to Figures 9, 13 and 17, although the magnitude of pressure coefficients is overestimated by the theory. This may be due to the error sources noted in Section 5.1. Rounding of the

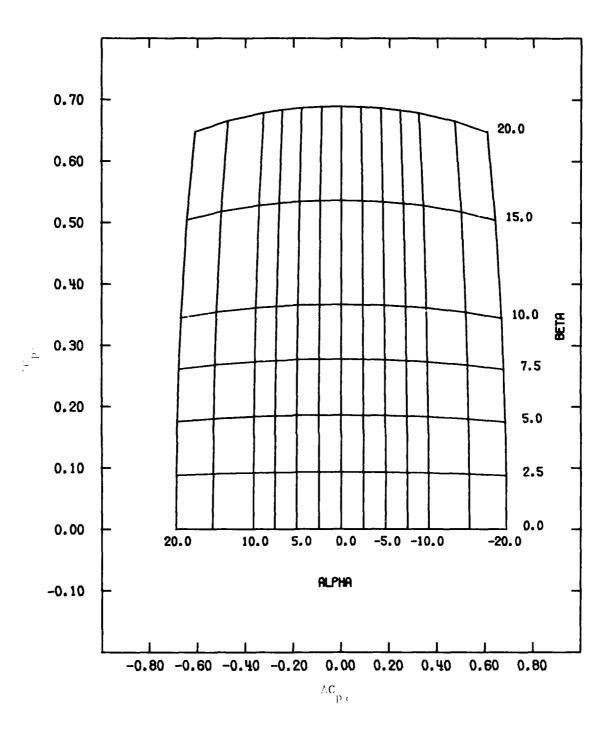


Figure 25. Angular Pressure Coefficients for a 30° Cone Probe,  $M_{\infty}$  = 0.20 and z/k = 0.68

pressure ports coupled with a slight misalignment of the ports, i.e., not normal to the local cone surface, may also contribute to the slightly overestimated values.

The experimental values are reasonably independent of Mach number as predicted with only slight variations over the Mach number range  $0.2 \le M_\infty \le 0.6$ . The angular functional relationships of equation (25) characterize the data up to  $\beta$  values of  $15^\circ$ . Beyond this point, the curves assume a double-lobed appearance which is probably due to flow separation.

### 5.3 Calibration Functions

The theoretically derived averaged pressure coefficient agrees well with experimental measurements carried out on large cones. The agreement – in an absolute sense – is, however, much poorer on the smaller cone probe. The functional variation with  $\alpha$  and  $\beta$  is correctly predicted by the theory but again the magnitude of change is slightly overestimated by the equations of Section 2.

The angular pressure coefficients of Section 2 exceed the measured values with the dependence of  $\Delta C_{p_{\alpha}}$  and  $\Delta C_{p_{\beta}}$  on  $\alpha,~\beta$  and  $M_{\infty}$  correctly represented by the theory. Since the functional relationships are correctly predicted by the slender body theory, the equations of Section 2 can be used as a tramework for a series of empirical calibration relations. These will take the form

$$\langle C_{p} \rangle = f_{1}(M_{co})\cos^{2}\alpha\cos^{2}\beta - C_{1}\sin^{2}\beta - C_{2}\sin^{2}\alpha\cos^{2}\beta$$

$$\Delta C_{p_{\alpha}} = C_{3}\sin^{2}\alpha\cos^{2}\beta$$

$$\Delta C_{p_{\beta}} = C_{4}\cos\alpha\sin^{2}\beta$$

$$C_{p_{\dagger}} = f_{2}(M_{co})\cos^{2}\alpha\cos^{2}\beta - C_{5}\sin^{2}\beta - C_{6}\sin^{2}\alpha\cos^{2}\beta$$

$$(38)$$

where  $f_1(M_\infty)$  and  $f_2(M_\infty)$  are functions of Mach number and  $C_1$ ,  $C_2$ ,  $C_3$ ,  $C_4$ ,  $C_5$  and  $C_6$  are constants. All of these parameters will depend on the body geometry.

Note that the functions of Section 2 are valid in a comparative sense, i.e., the effects of Mach number and body geometry on the pressure coeffi-

cients can be compared for a series of probes. This implies that the theoretical relationships can be used in the preliminary design of pressure probes white the final configuration must be calibrated.

#### SECTION VI

### GENERAL CHARACTERISTICS OF PRESSURE PROBES

#### 6.1 Introduction

The theoretical relationships of Section 2, while not capable of replacing individual probe calibrations, are suitable for evaluating sensor geometry and Mach number effects. Furthermore, effects of probe alignment on averaged and angular pressure coefficients can also be determined. These effects will be discussed in the ensuing sections.

6.2 Influence of Body Geometry and Mach Number on the Pressure Coefficients
As was noted in Section 5, the angular pressure coefficient is
primarily a function of body geometry and flow angle and is independent of
Mach number, i.e.,

$$\Delta C_{p_{\alpha}} = 4R' \sin 2\alpha \cos^2 \beta \tag{39}$$

Consequently, the sensitivity to flow angles is directly proportional to R' or dR/dz. For example, the angular sensitivity,  $\partial \Delta C_p/\partial \alpha$ , of a 40° included angle cone is 2.06 times greater than that for a 20° cone. It would then seem desirable to choose a large cone angle in an effort to improve angular sensitivity.

Since the probe is also to be used to measure total and static pressure, the effect of increasing cone included angle on these parameters must also be investigated. Calculations for a  $20^{\circ}$  and  $40^{\circ}$  cone have been carried out using equation (30) and these results are shown in Figures 26 and 27. These figures depict the variation of  $<\!C_p>$  with position,  $z/\ell$ , and Mach number. As can be seen,  $<\!C_p>$  increases with increasing conic angle as does the sensitivity to Mach number, i.e., at a given  $z/\ell$  location  $\partial<\!C_p>/\partial M_{\infty}$  increases with increasing cone angle. The latter infers greater Mach number dependence for the static and total pressure coefficients – an undesirable characteristic.

While increasing the cone angle increases the angular sensitivity, it also increases the Mach number sensitivity. Hence, a trade-off between

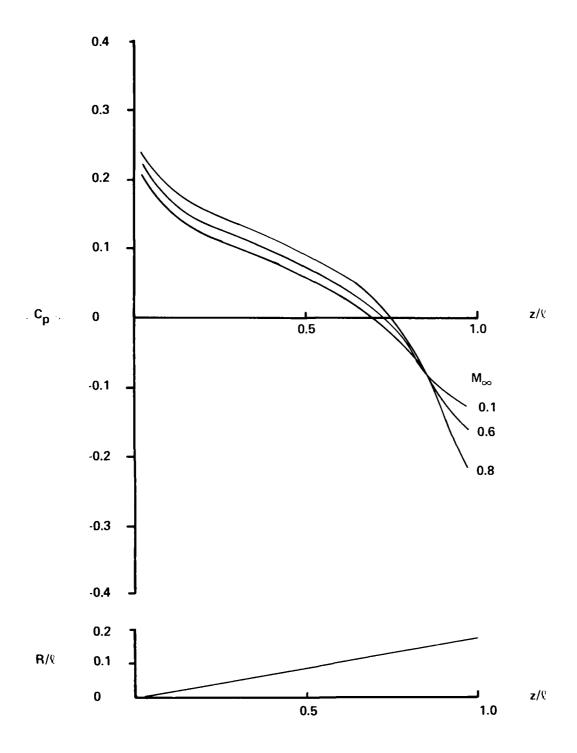


Figure 26. Calculated Averaged Pressure Coefficient for a  $20^{\rm O}$  Conic Section as a Function of Position and Mach Number

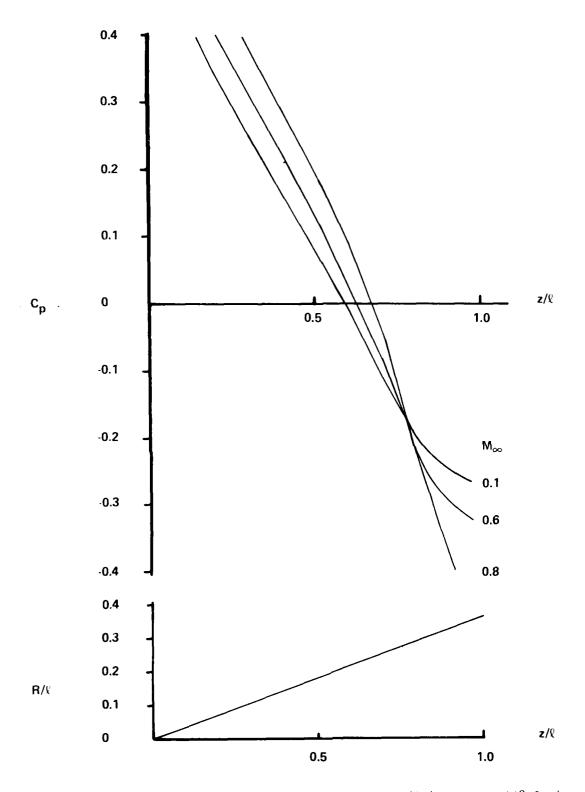


Figure 27. Calculated Averaged Pressure Coefficient tor a  $40^{\rm o}$  Conic Section as a Function of Position and Mach Number

angular and Mach number sensitivity must be made and the cone geometry selected for a given application, i.e., flow angle and Mach number range.

While flow direction probes are normally formed from either cones or hemispheres, other shapes may be used. Figures 28 and 29 show the variation of  $< C_p >$  with  $z/\ell$  and  $M_\infty$  for two bodies having

$$\frac{R}{\ell} = \sqrt{\frac{z}{\ell}} \tan \delta_c \tag{40}$$

so that dR/dz is equal to 1/2 the value for a cone of included angle  $2\frac{\delta}{c}$  at  $z=\ell$ .  $<\!C_p\!>$  tends to be much less sensitive to Mach number than the conic sections of Figures 22 and 26. At the same time, the angular sensitivity, dR/dz, is also reduced unless the static pressure ports are located well forward on the body, i.e.,  $z/\ell \sim 0.2$ . While this geometry appears to be superior to the cones, it might offer manufacturing difficulties since the static ports must be located in a region of fairly small radius. If a relatively large diameter probe can be used, this may pose no problem. Again, the sensor geometry must be chosen for a specific application in order to satisfy the trade-off between measurement accuracy and manufacturing difficulties.

6.3 Effect of Probe and/or Side Port Alignment on the Pressure Coefficients The influence of probe and/or side port alignment on the angular and averaged pressure coefficients can be ascertained from equations (25) and (29). The port locations denoted by  $\theta_i$  can be rotated relative to the design locations of  $0^{\circ}$ ,  $90^{\circ}$ ,  $180^{\circ}$  and  $270^{\circ}$  and the resulting coefficients computed.

Probe misalignments are of two types. The first consists of a manufacturing defect where one port is angularly or axially displaced relative to the other three static taps. A case of this type is plotted in Figures 30 and 31 for a 30° cone probe with one port displaced 2.5°, i.e.,  $\epsilon_i = 2.5^\circ$ ,  $90^\circ$ ,  $180^\circ$  and  $270^\circ$ . This results in a skewing of  $\Delta C_{p_\alpha}$  and  $\Delta C_{p_\beta}$  with  $\langle C_p \rangle$  also displaced. The nonlinearity in the differential pressure coefficients is quite obvious at the higher  $\alpha$  and  $\beta$  values.

The second misalignment consists of a rotation of the probe body itself relative to a fixed or predetermined coordinate system. This could occur

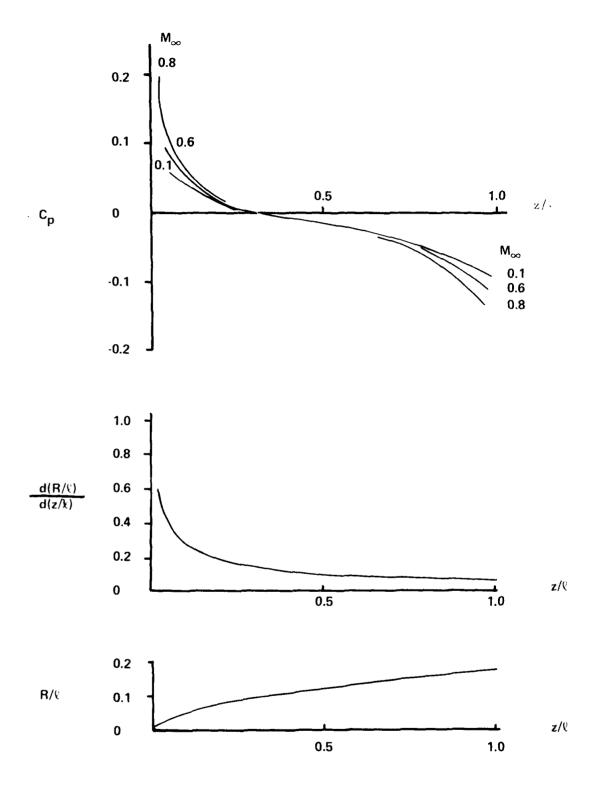


Figure 28. Calculated Averaged Pressure Coefficient for a 20° Rounded Cone as a Function of Position and Mach Number

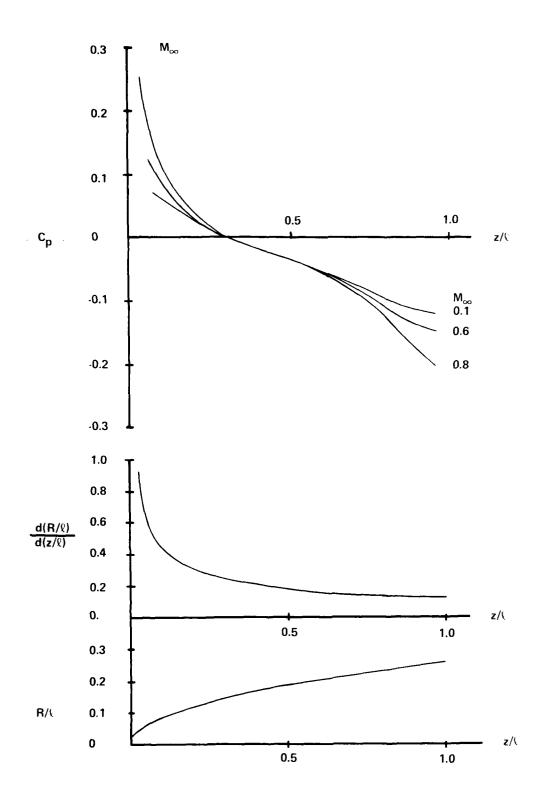


Figure 29. Calculated Averaged Pressure Coefficient for a  $30^{\rm O}$  Rounded Cone as a Function of Position and Mach Number

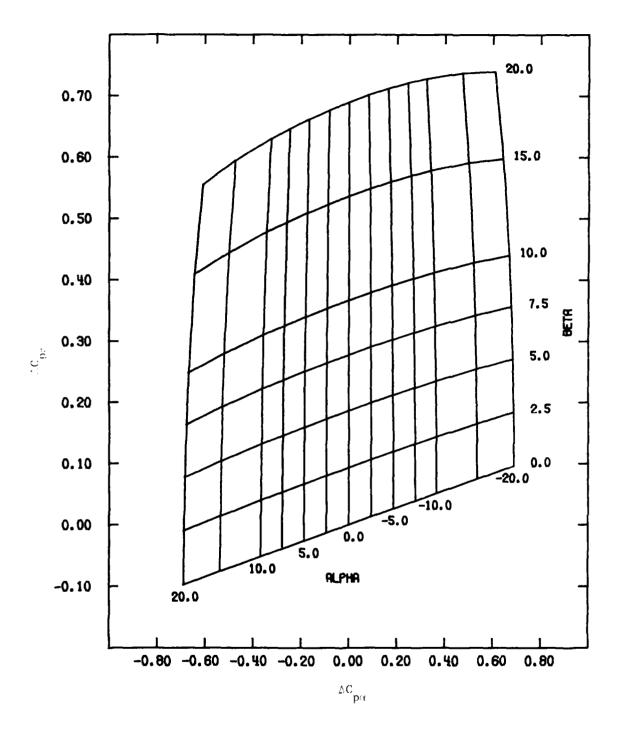


Figure 30. Angular Pressure Coefficients for a  $30^{\rm O}$  Cone Probe. Side Ports Located at  $\theta_1$  =  $2.5^{\rm O}$ ,  $90^{\rm O}$ ,  $180^{\rm O}$  and  $270^{\rm O}$ .  $z/\ell$  = 0.68 and  $M_{\infty}$  = 0.2

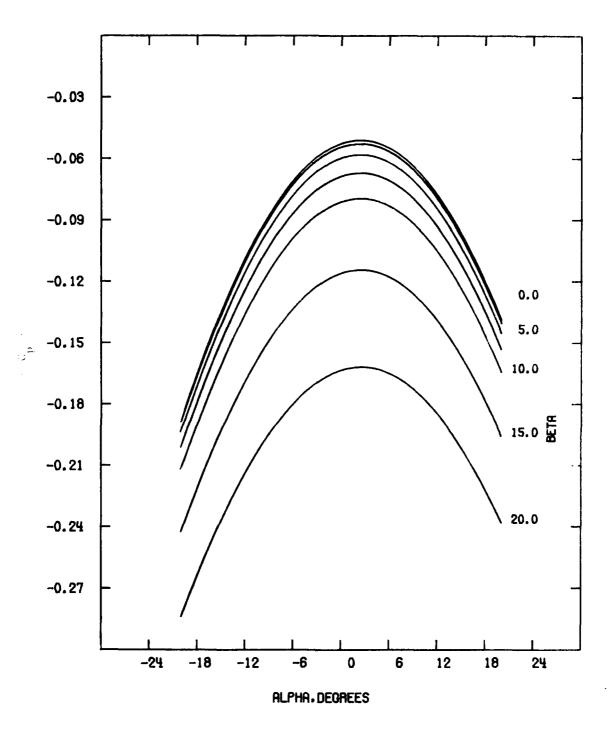


Figure 31. Averaged Pressure Coefficients for a  $30^{\rm O}$  Cone Probe. Side Ports Located at  $\theta_1$  =  $2.5^{\rm O}$ ,  $90^{\rm O}$ ,  $180^{\rm O}$  and  $270^{\rm O}$ .  $z/\ell$  = 0.68 and  $M_{\infty}$  = 0.2

in a turbomachine application during installation of the sensor. In this case, all  $\theta$  values are displaced by the same amount. The angular and averaged coefficients are plotted in Figures 32 and 33 for a port displacement of  $2.5^{\circ}$ . Note that  $\Delta c_{p_{\alpha}}$  and  $\Delta c_{p_{\beta}}$  are strongly influenced by the rotation, but  $<\!c_p\!>$  is unchanged.

The independence of  $<\!C_p\!>$  with regard to probe rotations can be employed to isolate probe manufacturing defects in the calibration process. If  $\triangle C_{p_\alpha}$  and  $\triangle C_{p_\beta}$  are skewed but  $<\!C_p\!>$  is symmetric with  $\alpha$  and/or  $\beta$ , then the probe is merely misaligned. If, however, both  $\triangle C_{p_\alpha}$  -  $\triangle C_{p_\beta}$  and  $<\!C_p\!>$  are skewed, then the probe ports are not normal to one another.

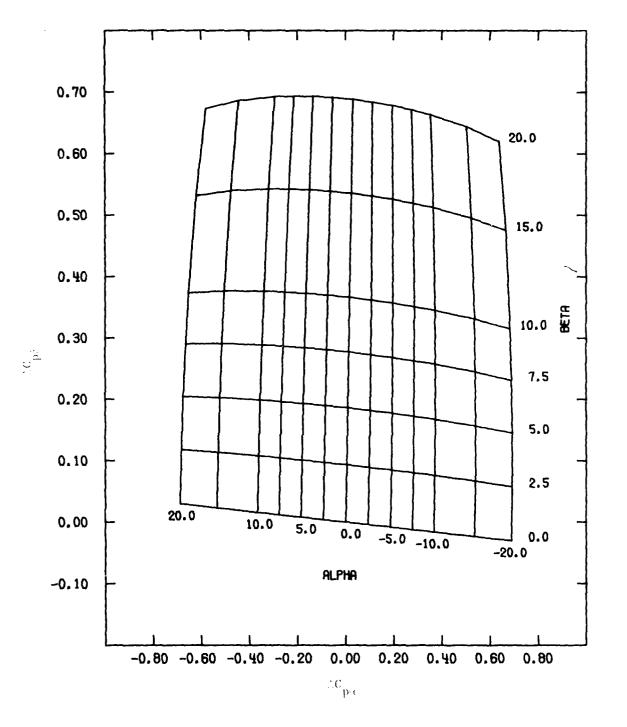


Figure 32. Angular Pressure Coefficients for a 30° Cone Probe. Side Ports Located at  $\theta_1$  = 2.5°, 92.5°, 182.5° and 272.5°. z/% = 0.68 and M<sub> $\infty$ </sub> = 0.2

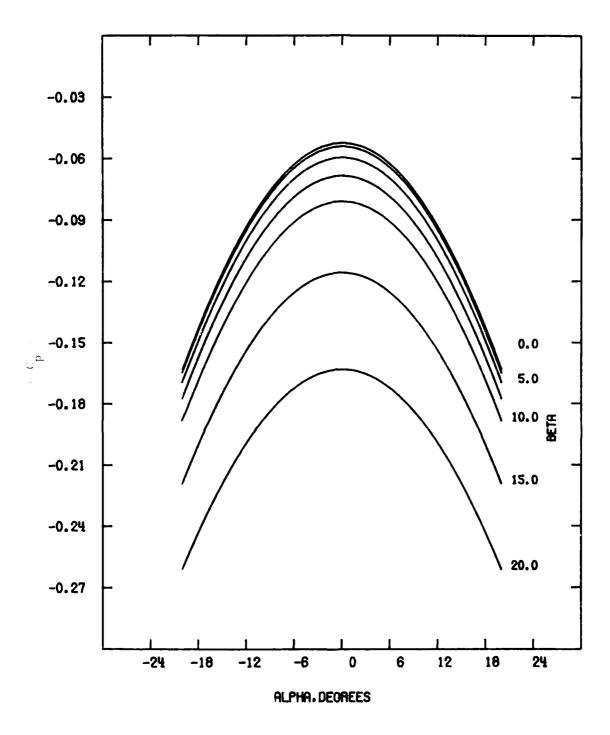


Figure 33. Averaged Pressure Coefficients for a 30° Cone Probe. Side Ports Located at  $\theta_1$  = 2.5°, 92.5°, 182.5° and 272.5°. z/% = 0.68 and M<sub>∞</sub> = 0.2

APPENDIX A

PROBE CALIBRATION DATA

See that the second of the sec

|                                      | (P) (10TAL)         | 1525.0     | 1716-0  | 2365-3       | 7266-3  | 0.5932         | 2266-0    | C-9932      | 2866-0   | 6365*3   | 0.9871   | C-9823  | 67-36-73   | 0.9360  |                     |     |               | (TCTAL)             | 3752-0       | C-9725  | 0.5891  | 2256.3  | 0.9934  | C.9936  | C. 5934     | 5665-3        | 7165-3    | C.5P82     | C. 9823 | 6.96.9  | 0.5227  |
|--------------------------------------|---------------------|------------|---------|--------------|---------|----------------|-----------|-------------|----------|----------|----------|---------|------------|---------|---------------------|-----|---------------|---------------------|--------------|---------|---------|---------|---------|---------|-------------|---------------|-----------|------------|---------|---------|---------|
|                                      | CAVERAGE)           | -0.0107    | C.C158  | 6.0357       | 0-0426  | 0.0478         | C.CS47    | 0.0539      | 0.0525   | 6.0494   | 0.0454   | 0.0394  | 0.0223     | 0,00-0- |                     |     |               | CAVERAGE)           | -6.6158      | 0.0139  | 0-0341  | 9170-0  | 0.0466  | 0.0489  | 5.0503      | 6670-0        | 69 70 " 3 | 0.0415     | 0.0355  | C.C159  | -c.cc98 |
| TEMPERATURE<br>CEG C<br>19.1         | CELTA CP            | -0.0230    | -0-0223 | -0.6252      | -0.0252 | -0.0263        | -0.0256   | -0.0256     | - 0.0263 | -0.0249  | -0.0233  | -6.0229 | -0.0204    | -0.0181 | MPERATURE           | ,   | ~             | CELTA CP            | 0.0312       | 0.0269  | 0.0255  | 0.0248  | 0.0232  | 0.0216  | 0.0222      | 0.0204        | 0.0209    | 0.0216     | 0.0213  | 0.0220  | C. 0257 |
| AVEFACE TEMP<br>res<br>19.1          | CELTA CP<br>(ALPHA) | -0-4327    | -0.3211 | -0.2111      | -0.1551 | 6260.0-        | -0.0578   | C-0118      | 0.0627   | 0.1196   | 0.1719   | 0.2254  | 0.3269     | 0.4357  | AVERACE TEMPERATURE |     | 16.2          | CELTA CP<br>(ALPPA) | -0.4200      | -6.3173 | -0.2666 | -0.1515 | 8720.0- | -0.0429 | 0.0095      | 6290-0        | 0.1173    | 0.1726     | 6-2253  | 0.3411  | 6-4475  |
|                                      | PS<br>CM H2C        | 785.525    | 187-299 | 786.611      | 789.103 | 789.469        | 189-614   | 785.776     | 789.678  | 789.491  | 789.539  | 789.090 | 787.595    | 785.961 |                     |     |               | CM PS               | 786.103      | 787.715 | 789.095 | 789.588 | 789-911 | 790.095 | 790.173     | 790.095       | 789.876   | 789.536    | 189.695 | 181.776 | 785-164 |
| AVERAGE RETROLCS<br>NUMBER<br>10495. | P4.                 | 787-595    | 787.931 | 788.428      | 788.737 | 789.112        | 789.565   | 196.105     | 780.067  | 791.256  | 192.268  | 793-064 | 794-154    | 195.854 | AVERAGE REYNOLES    |     | 10628         | P4 CM H2 C          | 787-688      | 787.968 | 783.413 | 788.728 | 189-699 | 789.523 | 7 90 - 00 3 | 790.562       | 791-195   | 791.863    | 792.579 | 794.261 | 195-942 |
|                                      | P 3                 | 785.569    | 787.730 | 769-697      | 765.587 | 789.975        | 790.166   | 756.262     | 790.184  | 759.976  | 7.65.588 | 789.531 | 787.987    | 186.309 |                     |     |               | P3 CM P20           | 785.505      | 787.159 | 786.605 | 789.112 | 789.466 | 789.675 | 149.745     | 189.102       | 249.691   | 789.121    | 788.684 | 781.352 | 185.671 |
| AVERACE MACH<br>NUMPER<br>0.186      | Cr H2C              | 556*562    | 794-132 | 792.485      | 791.716 | 566.362        | 190.676   | 185.879     | 789.412  | 786.955  | 786.955  | 788.663 | 187.857    | 787.443 | AVERACE MACH        |     | 9<br><br><br> | P2<br>CM H2C        | 195.750      | 550-462 | 192.374 | 191.641 | 196.961 | 746.346 | 785.820     | 789.352       | 726.937   | 146.544    | 188.241 | 787.766 | 167.342 |
|                                      | C# H20              | £07-055    | 607.703 | £08.000      | £08.048 | <b>608.066</b> | £66.675   | £ 08 . 07 9 | 666.670  | £ 66.031 | £08.328  | 608-232 | £67.556    | 866.938 |                     |     | r             | C# P1               | £ C6 - 9 5 6 | 607.624 | 607.934 | 608.060 | £08.078 | £C6.678 | 808.678     | £ C 8 . 6 7 B | £68.643   | 696-103    | £07.855 | ec7.436 | 866.533 |
| 8<br>0 0<br>0 0                      | PT<br>CP 526        | P CE - 297 | 806.279 | e ce . 1 a e | 608.168 | 8 06 - 19 7    | ec £ .205 | 868.216     | 604.201  | 808.808  | 808.576  | 908.572 | 80 6 . 231 | 802.275 | BETA<br>OFG         | , 1 | <b>د•</b> >   | CW F2C              | PC 6 . 16 1  | 808-152 | 808.143 | 808-200 | 806.295 | 808-200 | 808.205     | 806-209       | 608.249   | PC t . 196 | 808.196 | 506.187 | 9ce.183 |
|                                      | PS H 43             | 336.346    | 186.968 | 7ea.968      | 788.968 | 188.968        | 788.968   | 188.568     | 788.968  | 196.966  | 789.313  | 789.313 | 736.968    | 788.968 |                     |     |               | PS<br>C# H2C        | 768.568      | 786.968 | 788.968 | 188.568 | 788.968 | 788.968 | 788.968     | 788.968       | 783.368   | 186.966    | 788.968 | 189.968 | 166.568 |
|                                      | ALPHA<br>DE 6       | 7.05-      | -15.0   | -10.0        | -7.5    | -5.0           | -2.5      | 0           | 5.5      | 5.0      | 5.       | 0.01    | 15.0       | 20.0    |                     |     |               | ALPHA               | J. 35-       | -15.0   | -10.0   | -1.5    | -5.0    | -2.5    | 0-0         | 2.5           | 5.0       | 7.5        | 10.6    | 15.0    | 0.05    |

TABLE 1 (Cont'd) Pressure Coefficients for the Five-Ported, Conical Probe,  $M_{\parallel}=0.2$ 

|                              |        | ( TOTAL)     | 3425-3    | 7325 "3 | 6.96.3  | 7165.3  | 0.9927  | 1255.3  | 6.9954  | 0.9925  | C.9913     | C.9884    | 6-96-9  | 0.9605  | c.92ce  |                              |    |            | (TOTAL)   | 1738.3   | 6.9655     | 0.9849  | 0.9897  | \$155*3 | C. 9931 | C-5931   | 0.5931  | 6065.0  | C-9865  | 0.9866   | 6.9568  | 6.9169  |
|------------------------------|--------|--------------|-----------|---------|---------|---------|---------|---------|---------|---------|------------|-----------|---------|---------|---------|------------------------------|----|------------|-----------|----------|------------|---------|---------|---------|---------|----------|---------|---------|---------|----------|---------|---------|
|                              |        | (AVERAGE)    | -0.0121   | 6.119   | 0.0319  | 0.0392  | 5770    | C.C477  | 0670-0  | 0-0475  | C-0437     | 0343-3    | 0.0332  | C-0143  | -0-C144 |                              |    |            | (AVERAGE) | -6.0185  | C - CO F 7 | 6.0277  | 0.0345  | 0.0365  | C.C421  | 0.0430   | 6.6414  | 00.000  | 2550-0  | 0.029A   | 0.0086  | -6.6214 |
| MPERATURE<br>EG C            | ٠.     | DELTA CP     | C-0726    | 0.0763  | 4620-3  | 0.0780  | 0.0769  | 6.0753  | 0.0722  | 0.0729  | 0.6729     | 0.0726    | 0.0710  | C-0707  | 0.0663  | MPERATURE<br>EG C            |    | 4.         | DELTA CP  | 0.1266   | 0.1381     | 0-1390  | 0.1383  | 0.1361  | 0-1345  | C. i 326 | 0.1310  | 0.1303  | 0.1302  | 0.1279   | 0.1245  | C-1142  |
| AVERACE TEMPERATURE<br>DEG C | 17.5   | CELTA CP     | -0.4268   | -6-3259 | -0.2120 | -0.1529 | 2660-0- | -0.0462 | 6300-5  | 0.0590  | 0.1172     | 0.1687    | 0.2242  | 6.3377  | 0.4551  | AVERACE TEMPERATURE<br>0EG C | į. | 17.4       | CELTA CP  | -0-4505  | -0.3275    | -0-2149 | -0.1608 | -0.1023 | -0.0521 | 0.0 023  | 0.0560  | 0.1651  | 0.1618  | 6.2138   | 0.3354  | 0.4672  |
|                              |        | PS<br>CM H2C | 786.954   | 788.631 | 790.033 | 790.514 | 790.824 | 791-051 | 791-081 | 791-011 | 7 90. 793  | 524.067   | 789.640 | 788-378 | 785-540 |                              |    |            | CM P20    | 787.692  | 189.444    | 790-723 | 791-204 | 791.531 | 769-062 | 780.737  | 790-619 | 950-061 | 189.142 | 789-361  | 787.969 | 786-24C |
| AVERAGE REYNOLDS<br>NUPEER   | 10547. | P4 CM H20    | 787.810   | 788.085 | 788.544 | 788.698 | 789.265 | 189-681 | 796.164 | 796.701 | 791-326    | 792.025   | 792.387 | 794-012 | 195.750 | AVERAGE REYNOLDS<br>NUMBER   |    | 10532.     | 25H H2    | 787-129  | 787.706    | 788.234 | 788.527 | 783-880 | 788.257 | 788.750  | 789.305 | 789.550 | 790-262 | 196-973  | 192.024 | 194-371 |
|                              |        | CM #2C       | 785.561   | 787.168 | 788.509 | 789.016 | 789.378 | 789.605 | 769.706 | 789.614 | 789.396    | 7 8 5.051 | 788.282 | 247-625 | 765.335 |                              |    |            | CM #20    | 7 85.273 | 786.806    | 7:8.068 | 788.561 | 789.933 | 786.126 | 168.204  | 786-117 | 701.666 | 1+1.253 | 786.855  | 185.549 | 184.056 |
| AVERAGE PACH<br>NUMBER       | 0.185  | CHPE         | 195.998   | 194.276 | 792.614 | 791.E32 | 791-165 | 796.576 | 796.033 | 789.570 | 785.0EL    | 188.797   | 766.095 | 787.545 | 187.646 | AVERAGE FACH<br>Number       | •  | 0 - 185    | 25H 43    | 195-741  | 193.959    | 528-261 | 181.597 | 194.845 | 118.252 | 186.757  | 186.235 | 187.541 | 187.170 | 7Pt.FFE  | 166.213 | 165.456 |
|                              | c      | CH P.ZC      | EC 7 .230 | 867.925 | EC8.278 | £08.340 | £08.361 | £08.3£6 | £C#*5E5 | 808.348 | 60 E - 3CS | 808.222   | 807.768 | 607.353 | 806.576 |                              |    | <b>~</b>   | CP H2C    | FC7 .034 | £07.750    | £CE.126 | £08.213 | £08.248 | £C7-244 | £07.244  | £67.244 | £06.E65 | 806.791 | PCF. 577 | £22.334 | 194.602 |
| BETA                         | 0.2    | PT<br>C* H20 | 66.497    | 808-492 | 808.510 | £08.506 | 808.50i | 806.506 | e0e.353 | 608-492 | 808.471    | 808.444   | 806.005 | 838-108 | 808.091 | 8ETA<br>9E6                  | •  | <b>5-7</b> | CF H20    | 666.427  | P08.41C    | 8C8-414 | 808.410 | 8GE-41C | 867.575 | 807.375  | 867.375 | 307.640 | 807.648 | 807.C4E  | 867.048 | 150-104 |
|                              |        | CH H20       | 789.313   | 789.313 | 189.513 | 789.313 | 789.313 | 789.313 | 749.313 | 789-313 | 785.313    | 789.313   | 788.960 | 188.968 | 788.950 |                              |    |            | 05H M30   | 789.313  | 769.313    | 789.313 | 749.313 | 789.313 | 788-279 | 788.279  | 168.279 | 187.914 | 187.934 | 187.934  | 725-181 | 516-141 |
|                              |        | ALPHA<br>DEG | 2-52-     | -15.0   | -10.0   | -7.5    | -5.0    | -2.5    | 0.0     | 5.5     | 9.0        | 7.5       | 10.0    | 15.0    | 0-07    |                              |    |            | ALPHA     | 0-02-    | 0.51-      | -10.0   | -7.5    | 9-5-    | -2.5    | 0.0      | 5-5     | 5.0     | 1.5     | 10.0     | 15.9    | 20.0    |

with the contribution of the form of the same contribution to the form of the contribution of the same contribution of t

|                              |         | ( TOTAL)  | 6.5169      | 0.9568  | 1626-0  | 0.5855   | 0.9877   | 0.9893  | 9536.0  | 0.9887  | 0.9855  | 0.9812  | 0.9735  | 0.5490   | 5936-3  |                             |         |          | (TOTAL)            | 0.8662  | 0.9368  | 0.9590   | 6.9677   | 0.9725  | 9726-0   | 2425-3  | 0.9729  | 0.9677  | C.9EC®  | 0.9517  | 5.92CF  | 0.8814   |
|------------------------------|---------|-----------|-------------|---------|---------|----------|----------|---------|---------|---------|---------|---------|---------|----------|---------|-----------------------------|---------|----------|--------------------|---------|---------|----------|----------|---------|----------|---------|---------|---------|---------|---------|---------|----------|
|                              |         | CAVERAGE  | -6.0249     | 0.0052  | 0.6260  | C. C294  | 0.0331   | 0.0357  | 0-0368  | 0.0362  | C-0328  | 0.0282  | C-0228  | C. 00 34 | -0-0268 |                             |         |          | (AVERAGE)          | -0.0301 | -0.0075 | 0.0050   | C. CO 62 | 0.0115  | 0.0140   | C-C143  | 0.0121  | 6900-0  | 0.0038  | 0.0002  | -0.0150 | 1240-0-  |
| PERATURE                     | m       | DELTA CP  | C-1694      | 0.1946  | 0.2014  | 6.2015   | 0.1986   | 0.1970  | 0-1935  | 0.1913  | 0.1913  | C.1886  | 0.1858  | 0.1763   | 0-1579  | PERATURE                    | ,       | <b>1</b> | OLLTA CP           | 2+92-3  | 0-3041  | 0.3183   | 0.3208   | 0.3177  | 0.3107   | 0.3068  | 0.3052  | 6.3079  | 0, 3071 | 0.3012  | 0.2816  | 0.2419   |
| AVERAGE TEMPERATURE<br>DEG C | 19.3    | CELTA CP  | -0.4713     | -0.3322 | -0.2323 | -0-1663  | -0-1128  | -0.0588 | 9,00-0- | 0.0478  | 0.1020  | 0.1555  | 9602-0  | 0.3274   | 0.4736  | AVERAGE TEMPERATURE         | 16.5    |          | CELTA CP           | -0.4585 | -0.3260 | -0.2252  | -0.1753  | -0.1247 | -0.0741  | -0.0184 | 0.0330  | C.08E8  | 6-1417  | 0.1890  | 0.3062  | 99440    |
| S                            |         | CN H2C    | 787.924     | 789.937 | 791.261 | 791.754  | 792-666  | 792.243 | 791.938 | 791.566 | 791.266 | 790.908 | 790-427 | 789.673  | 787.239 |                             |         |          | P5<br>(# F20       | 780.689 | 182.622 | 783.926  | 784.369  | 784.669 | 784-821  | 784-873 | 784.747 | 184.486 | 184.126 | 183.691 | 182.281 | 786-316  |
| AVERAGE REYNULD<br>NUMBER    | 10479.  | CM H20    | 736.160     | 786.876 | 787.378 | 187 -649 | 187.977  | 788-396 | 788.540 | 788.756 | 789.379 | 790.052 | 790.820 | 192.488  | 794.296 | AVERAGE REYNDLUS<br>Albypfr | 10504.  |          | ) 2H H3            | 776.326 | 776-895 | 777.160  | 777.338  | 111-612 | 117.968  | 778-438 | 178.955 | 119.5/6 | 730.316 | 781.006 | 182-196 | 784.677  |
|                              |         | C# #20    | 784.675     | 786.199 | 182.181 | 787.881  | 7 86.239 | 788.453 | 788.213 | 787-820 | 787.580 | 767.274 | 786.846 | 785.637  | 784.195 |                             |         |          | CM #20             | 775-652 | 776.834 | 777.882  | 118.211  | 178.638 | 778-920  | 179.026 | 118.524 | 778.612 | 778.268 | 215-111 | 776.878 | 775.683  |
| AVERAGE TACH<br>Number       | C - 186 | CF H20    | 195.200     | 193.256 | 791.841 | 359.062  | 796.147  | 185.527 | 788.632 | 787.829 | 787.414 | 387.656 | 186.781 | 786.178  | 785.165 | AVERAGE PACH                | C • 186 |          | C# P2              | 785.064 | 783.100 | 761.436  | 780.667  | 775.986 | 775.376  | 776.796 | 778.325 | 111.882 | 111.606 | 177.399 | 176-911 | 776-1155 |
|                              | 0       | C# H30    | 866.554     | £07-344 | 607.781 | 516.503  | £C7.973  | £06.008 | 607.672 | 807-323 | 807.256 | 667.179 | EG7.039 | 606.572  | 165.755 |                             |         |          | CM H20             | 196.896 | 231.161 | 198.217  | 198.302  | 196.469 | 796.512  | 198-864 | 198.565 | 198.469 | 758.334 | 798-169 | 197.596 | 196.216  |
| 6 E T A<br>D E G             | 0 - 0 1 | CM H20    | 80 4 . 14 6 | 608-174 | 508.183 | FOR. 191 | e00-00a  | 608.213 | 867.673 | 807.541 | 867.546 | PO7.541 | 807.550 | 867.555  | 667.559 | 8<br>36<br>30<br>30         | 15.0    |          | CH H20             | 195-561 | 885-862 | 194.995  | 266-362  | 196.996 | 666. H21 | 799.080 | 280.661 | 980-56/ | 199.082 | 063-662 | 195.158 | 795-134  |
|                              |         | P.S. H.20 | 786.968     | 436.95₺ | 186.966 | 388.984  | 188.188  | 188.968 | 156.623 | 786.279 | 168.279 | 188.279 | 788.279 | 188.279  | 788.279 |                             |         |          | P S CM H 2G        | 180.006 | 780.006 | 1.60.536 | 186.006  | 160.006 | 136.006  | 780.006 | 186.006 | 300-387 | 780-006 | 180.006 | 786.036 | 780.006  |
|                              |         | ALPHA     | J*97-       | -15.6   | -10.0   | -7.5     | -5.9     | -2.5    | 0.0     | 5.5     | 5.0     | 7.5     | 10.0    | 15.0     | 20.0    |                             |         |          | A L P H 4<br>U E G | -20.0   | -15.0   | -10.0    | -7.5     | 2.6     | -2.5     | ) • O   | 5.5     | 2.0     | 7.5     | 10.0    | 15.0    | 20.0     |

TABLE 1 (Cont's) Pressure Coefficients for the Five-Portes, Conical Probe,  $M_{\rm p} \approx 0.2$ 

|              |         | 9 E F A<br>0 E G |         | AVERAGE PACH | ±.      | AVERACE RETROLCS<br>NUMBEER | ROLES   | AVERAGE TEMPERATURE | MPERATURE<br>EG C |                   |         |
|--------------|---------|------------------|---------|--------------|---------|-----------------------------|---------|---------------------|-------------------|-------------------|---------|
|              |         | 20.0             |         | 0.186        |         | 10479.                      |         | 17                  | 17.0              |                   |         |
| ALPHA<br>CEG | DSH MO  | CF H20           | C# 420  | CH PRZE      | CP F20  | 04 H3                       | C# P520 | CH AZC ELLALE       |                   | DELLASP (AVERAGE) | CTOTAL  |
| 0.02         | 780.351 | 799.431          | 112.952 | 163.940      | 175.541 | 175-593                     | 782.719 | -0.4375             |                   | -0.0473           | 0.8365  |
| 15.0         | 780-351 | 709.413          | 197.232 | 181-126      | 776.536 | 175.964                     | 784.631 | -0.3118             | 0.4247            | -0.0305           | 0-8856  |
| -10.0        | 786.351 | 504-552          | 157.788 | 786.155      | 177.288 | 776.006                     | 786.021 |                     | 0.4584            | -6.6254           | C. 9152 |
| 1.5          |         | 209-662          | 197.975 | 779.356      | 777.805 | 776.032                     | 786.491 | -0.1745             | 6.4559            | -0-6226           | 6.9250  |
| 0.0          | 790.351 | 262.662          | 515.161 | 178.669      | 778.474 | 176.254                     | 786.730 | 786-730 -0-1278     | 0.4368            | - 6.0169          | 0.9324  |
| 5 * 2        |         | 755.714          | 198.489 | 770.386      | 179.240 | 776.850                     | 787.235 | 787-235 -0.0864     | 0.4204            | -6.0142           | 6.9256  |
| 0:           | 781.640 | 860°038          | 758.885 | 17E-177      | 775.719 | 177.606                     | 787.593 | 787.593 -0.0259     | 0.4141            | -0.0140           | 0.9383  |
| 5.           | 781.739 | 999*008          | 655.662 | 778-415      | 786-331 | 778.810                     | 786-130 | 0.0201              | 0.4119            | -6.0162           | 0.9358  |
| 0.           | 782.419 | 801-394          | £00°003 | 178.182      | 786.585 | 780.073                     | 788.580 | 0-0680              | 6.4213            | -0.0216           | C-927C  |
| • 5          | 182.419 | 861-399          | 199.856 | 176.5CE      | 525.511 | 780.781                     | 786.168 | 0.1197              | 0.4343            | -0.0302           | 0.9171  |
| 10.0         |         | 861-412          | 629.652 | 778.356      | 779.390 | 781-494                     | 787.655 | 0.1652              | 1587-0            | -0.0366           | 4936.0  |
| 15.0         | 182.419 | 801-507          | 199-196 | 178-174      | 776.565 | 763.336                     | 786-117 | 0.2764              | 0.3956            | -0-6456           | 0-8789  |
| 50.0         | 782-419 | 801-512          | 198.205 | 177-474      | 777.518 | 785.382                     | 784.175 |                     | 0.3487            | 0.3487 -0.0671    | 5.8270  |

|                            |        | CP CP (TOTAL) | -0.0421 6.5476 | -0.0055 0.9948 | C.0209 C.5992 | 0.0300 1.0000 | 0.0367 1.0000 | 0.0415 1.0000 | 0.0425 1.0000 | 0.0423 1.0000 | 0.0463 1.0000 | 0.0344 1.0000 | C.0253 C.9948 | 7755°3 3700°0 | -6.6265 0.5412 |                              |             |        | CP CP CP CAVERAGE) (TOTAL) | -0.0396 0.9512 | 2266-3 3700-3- | C. C212 0.9977 | 0.0299 1.0000 | 0.0364 0.9589 | 0000-1 60,000 | 0.0394 1.0000 | 0.6412 1.666 | 0.0383 0.9977 | 0.0318 0.9970 | C-0248 0-9941 | C. CO35 0.9918 |
|----------------------------|--------|---------------|----------------|----------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|----------------|------------------------------|-------------|--------|----------------------------|----------------|----------------|----------------|---------------|---------------|---------------|---------------|--------------|---------------|---------------|---------------|----------------|
| TEMPERATURE<br>CEG C       | 15.0   | CELTA CP      | -0.0254        | -0-0201        | -C.0182       | -0.0204       | -6-0213       | -C.0232       | -0.0237       | -0.0242       | -0.0237       | -0.6230       | -C.0281       | -0.0212       | -0.0224        | MPERATURE<br>EG C            | ر<br>د<br>د | 14.5   | DELTA CP<br>(BETA)         | 0-0344         | 0.0399         | 0.0380         | 0.0364        | 0.0333        | 0.0313        | 6.0330        | 0.0311       | 0.0295        | 0.0313        | 0.0315        | 0.0301         |
| AVERACE TE                 | 5      | CELTA CP      | 7777-0-        | -0-3246        | -0.2062       | -0.1492       | -0.0930       | -0.0356       | 0.0158        | 7220-0        | 0-1324        | 0.1657        | 0.2470        | 0.3599        | 24240          | AVEFACE TEMPERATURE<br>CEG C | ט           | 71     | CELTA CP                   | -0.4432        | -0-3269        | -0.2116        | 7271.0-       | +960.0-       | -0.0385       | 0.0009        | 6.0747       | 0.1298        | 0-1913        | 0.2436        | 0.3580         |
| ROLDS                      |        | C# 420        | 763.459        | 773.662        | 781.202       | 783.859       | 765.750       | 786.837       | 786.403       | 786.157       | 785.136       | 182.967       | 781.042       | 773.325       | 105.597        | ROLES                        | r.          |        | PS<br>CM H2G               | 164.671        | 774.776        | 781.980        | 791-618       | 786.376       | 787.368       | 787-737       | 787-368      | 786.626       | 791-676       | 789.332       | 182-676        |
| AVERAGE REYNDLUS<br>NUMBER | 23798. | F4<br>CH H20  | 775.181        | 777.639        | 780.484       | 782.129       | 784.048       | 786.411       | 788.180       | 791-025       | 794.220       | 197.288       | 802 - 10 4    | 806.113       | 816.508        | AVERAGE REYNOLDS<br>NUMBER   | NO N        | 23898  | P4<br>CM H20               | 113.226        | 775.353        | 778.066        | 787.214       | 781.583       | 784.003       | 785.638       | 789-287      | 192.657       | 803-304       | 806.915       | 814.610        |
|                            |        | P 3 CM 7 20   | 765.822        | 175.521        | 762.585       | 785.750       | 787.716       | 788.983       | 788.595       | 768-397       | 787-320       | 162.054       | 783.651       | 175-291       | 766.481        |                              |             |        | CP H20                     | 761.485        | 271.696        | 778.463        | 7 58.443      | 783.303       | 164.476       | 784.683       | 784.494      | 783.503       | 788.745       | 7 66. 363     | 779.178        |
| AVERAGE PACH               | 6.402  | C# 42         | e16.473        | 667.733        | 341.661       | 195.940       | 792.650       | 789.701       | 786.346       | 783.869       | 781-997       | 132.211       | 179-161       | 774-715       | 172.436        | AVERAGE PACH<br>NUMBER       | NUMBER      | 0 -403 | CP H2C                     | 814.253        | #C5.594        | 529-161        | 600-865       | 196.486       | 187.557       | 784.816       | 182.386      | 780.661       | 785.406       | 783-996       | 781.372        |
|                            | Ģ      | CH H20        | 672.192        | 124-918        | 676.576       | 616.709       | 878.639       | 616.639       | 149.273       | 475.881       | 675.742       | £75.397       | 876.535       | 674.708       | 869.868        |                              |             | νį     | DZH 43                     | e7C-124        | 674.363        | £74.293        | EB1.949       | 674.328       | 674.432       | 174.552       | 674.562      | 874.636       | 182.574       | £82.852       | 861.393        |
| 8<br>1<br>0<br>6<br>6      | 0      | PT<br>CM H20  | 677.656        | 876.917        | 876.639       | 876.709       | 876.639       | 876.639       | 875.881       | 875.881       | 875.742       | 161.2197      | 877.022       | 675-229       | 875.264        | BETA                         | 30 ·        | 2.5    | P1<br>CF H20               | 874.641        | 874.571        | 874.502        | 881.949       | 874-432       | 874-432       | 8/4.502       | 874.502      | 874.847       | 682.852       | B83.408       | 151.288        |
|                            |        | CM H20        | 784.142        | 784-145        | 784.142       | 784.142       | 184.142       | 184.142       | 783.453       | 783.453       | 783.453       | 783.108       | 784.142       | 782.419       | 782.419        |                              |             |        | CM H2G                     | 782-074        | 185.674        | 762.074        | 789.313       | 782.074       | 782.074       | 182.674       | 782.074      | 782-419       | 789.313       | 789-313       | 789.313        |
|                            |        | ALPHA<br>Of 6 | -20.0          | -15.3          | 0.01-         | -7.5          | -5.0          | -2.5          | 0.0           | 2.5           | 5.0           | 7.5           | 10.0          | 15.0          | 20.0           |                              |             |        | ALPHA<br>DEG               | -50-0          | -15.0          | 0.01-          | -7.5          | -5.9          | -2.5          | 0.0           | 5.5          | 5.0           | 7.5           | 10.0          | 15.0           |

|         | ~           | 5.0      |              |           |                         |          |                     |           |           |         |
|---------|-------------|----------|--------------|-----------|-------------------------|----------|---------------------|-----------|-----------|---------|
|         |             |          | -<br>-<br>-  |           | 24000                   |          | 7.                  | 14.2      |           |         |
| CH H 2C | CP H20      | C# #20   | CM HZC       | CH F20    | CM 420                  | CM H20   | DELLAGE             | DELTA CP  | CAVERAGE  | (TOTAL) |
| 169.067 | 883.649     | 676.880  | 622.161      | 768.098   | 782.987                 | 776-634  | -0.4242             | 0.0924    | -0-0349   | 0-9549  |
| 169-062 | 883.049     | 882.471  | e13.663      | 177.476   | 782.647                 | 786.390  | -6.3358             | 0.0965    | -0.0070   | 0.65.0  |
| 169.067 | 883.188     | £82.771  | 805-439      | 765.019   | 785.587                 | 793.716  | -0.2146             | 0.60.0    | 0.0169    | 6.9955  |
| 169.06/ | 883.119     | 683.649  | 801-780      | 7€7.723   | 787.364                 | 796-174  | -0.1560             | 0.0914    | 0.6278    | 0.9992  |
| 169.062 | 883.119     | 683.049  | 198.594      | 789.746   | 789.283                 | 197.781  | -0.1007             | 6980.0    | 0.0342    | 2665*3  |
| 791-361 | 883-139     | £83.739  | 796.268      | 751.381   | 792-317                 | 199.492  | -0-0428             | C.0878    | 6.6377    | 1.0000  |
| 791.381 | 683.739     | 693-739  | 193.366      | 791.529   | 795-067                 | 799.813  | 0.0184              | 0.0854    | 0-0357    | 1.0000  |
| 791.381 | 863.606     | 683.739  | 791-362      | 791-551   | 197-162                 | 799.359  | 6.0692              | C-0845    | 0-0392    | 2656-0  |
| 791.381 | 883.808     | 683.739  | 78ê.715      | 796.530   | 806.995                 | 7 96.130 | 0.1329              | 0.0822    | 0-0347    | 2666-3  |
| 791.381 | 883.547     | 863.600  | 786.615      | 788.828   | 804.180                 | 796.485  | 0.1876              | 0.0827    | 0.0291    | 0.9962  |
| 191.361 | 864.156     | 663.600  | 785.000      | 786.238   | 608-600                 | 793.479  | 0.2473              | 0.0781    | C-C194    | 3756-3  |
| 791.381 | 864.295     | 683.669  | 781.757      | 778.411   | 816.148                 | 786.985  | 0.3761              | 0.0923    | 2000-0-   | C-9933  |
| 791.381 | 884.503     | 679.847  | 780.037      | 770-517   | 824.647                 | 175.962  | 0.4790              | 0.0585    | -0.0386   | 2056-2  |
|         | BEIA<br>DEG |          | AVERAGE MACH | 1         | AVERAGE REYNOLES NUMBER | ROLES    | AVERAGE TEMPERATURE | MPERATURE |           |         |
|         | 7.5         |          | 0.401        |           | 23935                   | ŧ .      | 15                  | 15.0      |           |         |
|         |             |          |              |           |                         |          |                     |           |           |         |
| CH H 20 | CH H20      | CF H23   | CH H2C       | CH H20    | P4<br>CM H20            | CH 420   | CELTA CP            | DELTA CP  | CAVERAGE) | CTOTAL  |
| 791.036 | 883.672     | 679.502  | £21.504      | 7 66. 164 | 778.454                 | 780-656  | -0-4647             | 0.1564    | 6940-0-   | C-9550  |
| 791.936 | 883.672     | 883.116  | 612.731      | 775.608   | 780.448                 | 790-705  | -6.3485             | 0.1630    | -6.0126   | 0.9940  |
| 791°C36 | 883.672     | 883.116  | 8 04 - 157   | 7 83.275  | 783.984                 | 798.192  | -0.2178             | 0-1610    | 0.0147    | 3465-3  |
| 731.036 | 883.672     | e83.325  | 80C.631      | 7 85.856  | 785.572                 | 334.038  | -6-1626             | 0.1579    | 0.0227    | 0.9962  |
| 791.030 | 883.672     | 663.533  | 197-143      | 787.516   | 787.529                 | 802.153  | -0.1036             | 0.1537    | 0.0286    | 0.9985  |
| 791-036 | 883.672     | EB 3.672 | 794.061      | 788.758   | 789.798                 | 803.042  | 9940-0-             | C-1542    | 0.0311    | 1.0000  |
| 791.636 | 883.672     | 883.672  | 791-225      | 789.259   | 792.359                 | 803.325  | 0.0122              | 0.1518    | 0.0325    | 1.0000  |
| 791.036 | 883.672     | 683.672  | 768.985      | 7 88.956  | 795.025                 | 862.834  | C-0652              | 0.1498    | 0.0315    | 1.0000  |
| 192-162 | 884.017     | E83.906  | 767.076      | 788.261   | 798.773                 | 801.968  | 0.1263              | 0.1480    | 0.0285    | 2266-3  |
| 191-161 | 884.017     | 838.83   | 785.331      | 786.485   | 802.157                 | 800-248  | 0.1816              | 0.1488    | 6. 6234   | 2.6977  |
| 791.381 | 110-488     | E83.6CC  | 183.676      | 783.588   | 805.797                 | 051.161  | 0.2388              | 0.1490    | 0.0155    | 0.9955  |
| 191.381 | 884.920     | 883.530  | 175.819      | 777.182   | 814.125                 | 790.577  | 6.3668              | 0.1432    | -0.0102   | 0.5851  |
| 791-341 | 884.926     | E75.50C  | 775.825      | 768-107   | 823.503                 | 780.538  | 0.5096              | 0.17.0    | 0 3 7 4   | C.9421  |

|              |              | BETA<br>DEG  |               | AVERAGE MACH<br>NIMBER | <u>1</u>      | AVERAGE REYNOLDS<br>NUMBER | ROLES        | AVEFACE TEMPERATURE<br>DEG C | MP ERA TURE<br>EG C |              |   |
|--------------|--------------|--------------|---------------|------------------------|---------------|----------------------------|--------------|------------------------------|---------------------|--------------|---|
|              |              | 10.0         | 0.            | 0.402                  |               | 24135.                     |              | 14.1                         | <del>-</del> :      |              |   |
| ALPHA<br>EEG | PS<br>CM H2G | PF<br>CP H20 | 02H M3        | P Ž<br>CP H2C          | P3<br>CM P20  | P 4<br>CM H20              | P5<br>CM H26 | CELTA CP<br>(ALPHA)          | DELTA CP<br>(SETA)  | (AVERAGE)    | ( 101AL )                               |
| J-25-        | 791.381      | 686.519      | 679.986       | £20.96C                | 765.346       | 773.873                    | 784-489      | 6767-0-                      | 0.2012              | -0.0546      | C - 5 2 1 3                             |
| -15.0        | 191.381      | PA5-129      | 884.686       | 811.214                | 774.658       | 178.477                    | 754.812      | -0.3492                      | 0.2150              | -0.0170      | 0.9889                                  |
| 0-01-        | 191.381      | 384.607      | 664-595       | e02-649                | 781-994       | 781.814                    | 802.082      | -0.2235                      | C.2155              | C.00e1       | 0.9966                                  |
| -1.5         | 191.725      | 885.656      | 885.058       | 195.361                | 184.957       | 783.614                    | 804.780      | -0-1681                      | 0.2124              | 6-0154       | 1.0000                                  |
| -5.9         | 192.079      | 885.610      | 635-610       | 196.031                | 787.239       | 785.973                    | 806-789      | -0.1075                      | 0.5090              | 0.0267       | 1.0000                                  |
| -2.5         | 132.610      | 684.776      | 684.776       | 793.362                | 788.071       | 788.175                    | 807-507      | -0.0529                      | 0.2097              | 0- C231      | 1.0000                                  |
| 0.0          | 192.415      | ees.19C      | 865.190       | 796.628                | 789.087       | 791.072                    | 8C6.C79      | 0.0048                       | 0.2047              | C-0248       | 1.0000                                  |
| 5.5          | 792.415      | 885.329      | 885.259       | 786-123                | 7 € 8 • 7 6 9 | 793.875                    | 807.502      | 0.0620                       | 0.2023              | 0.0233       | 0-9993                                  |
| 2.6          | 192.415      | 685-389      | EE5.259       | 786.024                | 787.584       | 797.018                    | 806.377      | 0.1183                       | 0.2023              | C-C19 e      | 1666 0                                  |
| 7.5          | 792.415      | 965.468      | £85.468       | 784.153                | 785.760       | 800.715                    | 804.477      | 0.1760                       | C.2011              | 0.0146       | 1.0000                                  |
| 0.01         | 192.415      | 865-468      | 685-468       | 782.583                | 783.415       | 804.288                    | 802.038      | 0.2323                       | 0.2001              | 6.0072       | 1-0000                                  |
| 15.0         | 792.415      | 885.885      | 664.678       | 513.677                | 776.769       | 812-768                    | 194-684      | 0.3611                       | 2161.0              | - 0. 0172    | 0.9607                                  |
| 20.0         | 192.415      | 686.441      | 686.464       | 173.423                | 768.347       | 822.108                    | 784.956      | 0.5178                       | 0.1766              | -0-0554      | 0.9364                                  |
|              |              | BET<br>DE    | <b>⋖</b> ∪    | AVERAGE MACH<br>Number | <u>.</u>      | AVERAGE REYNOLDS           | NO LES       | AVEFACE TE                   | TEMPERATURE         |              |   |
|              |              | 15.0         | 0             | 0.401                  |               | 23945                      |              | 15.0                         | ,                   |              |   |
| ALPHA<br>Cec | CP HSC       | CP H20       | P1<br>CM H2C  | P.Z.<br>CP H2C         | CH H20        | CM P4                      | P5<br>CM H20 | CELTA CP<br>(ALPHA)          | DELTA CP            | C PO PO CE O | ( P) |
| -20.3        | 191.725      | 864.153      | 874.978       | 614.669                | 767.355       | 168.924                    | 793.643      | 6464-0-                      | 0.2866              | -C.059E      | 0.8910                                  |
| -15.0        | 191.725      | 883.597      | 278.678       | 665.433                | 773.677       | 173.594                    | 803.504      | -0.3466                      | 0.3225              | -0.0286      | 0.9399                                  |
| -10-0        | 191.725      | 884-431      | 1111          | 776.859                | 179.559       | 775.305                    | 810.679      | -6.2325                      | 0.3357              | -0.0121      | C. 9858                                 |
| -7.5         | 791.125      | 384-431      | E 8 3. 805    | 192.954                | 781.818       | 776-458                    | 612.995      | -0.1779                      | 0.3363              | -0-0072      | 0.9933                                  |
| -5.0         | 791-725      | 664.431      | 883.605       | 185-296                | 783.699       | 778.141                    | 814-445      | -0.1203                      | 6.3316              | -0-0036      | 0.9933                                  |
| -2.5         | 191-125      | •            | £ 8 3 • 8 C 5 | 186.146                | 784.872       | 780.173                    | 815.189      | -0.0644                      | 0.3270              | -0-0014      | £266.3                                  |
| 0.0          | 196.376      | EP4.845      | £84.150       | 763.581                | 785-850       | 783.089                    | 815.552      | -0.0653                      | C-3202              | 9000-0-      | 6.9925                                  |
| 2.5          | 192.070      | 884.915      | 684.150       | 781-057                | 785-235       | 785-963                    | 814.871      | 0.0528                       | 0.3192              | -0-0031      | 0.9918                                  |
| 5.0          | 191-725      | 664.109      | £83.E05       | 178.706                | 783.265       | 786-937                    | 813.307      | 0.1100                       | 0.3231              | -0-0072      | 2365.0                                  |
| 7.5          | 791.725      | 884-709      | 683.865       | 177.001                | 781.355       | 792.812                    | 811.22B      | 0.1700                       | 0.3213              | -0.0121      | C-9903                                  |
| 10.0         | 191.725      | 864-848      | 283.111       | 775-001                | 179.549       | 796.320                    | 808.760      | 0.2193                       | 0.3137              | -6.0171      | 0.9613                                  |
| 15.0         | 791-725      | 949.489      | F80.157       | 17 1-1 21              | 173.499       | 805-234                    | 806-971      | 0.3448                       | 0.2950              | -0.C37P      | 9546.3                                  |
| 29.0         | 791-725      | 186.4987     | 674.526       | 533-292                | 767-024       | 814.867                    | 536.062      | 0.5132                       | 0.2568              | -0.0725      | 0.8879                                  |

TABLE 2 (Cont'd) Pressure Coefficients for the Five-Ported, Conical Probe,  $M_{\rm p}=6.4$ 

|                                      | E) (10[AL)         | 5 0.8434 |                 | 6 0.9431  | 5 0.9536        | 8 C-9596 | 5 0.9622 | 2 0.9625 | 8 0.9592      | 1 0.9547 | 0 0.9461 | 1 0.9356 | 6 0.8963 | 1 0.8323 |
|--------------------------------------|--------------------|----------|-----------------|-----------|-----------------|----------|----------|----------|---------------|----------|----------|----------|----------|----------|
|                                      | CAVERAG            | -6.6175  | -C.C551         | -0-0468   | -0.0405         | -0.0358  | -0.6345  | -C.C352  | -0.0368       | -0.0421  | -0.0520  | -0-0591  | 9690-0-  | -0-1001  |
| TEMPERATURE<br>TEG C<br>15.0         | DELTA CP CAVERAGE) | 0.4144   | 0.4634          | 0.4831    | 0.4688          | 0.4514   | 0-4398   | C.4351   | C-4298        | 0.4363   | 0.4572   | 0.4615   | 6727-3   | 0.3838   |
| AVERACE TEMPERATURE<br>15.0          | CH HZC CALPLAS     | -0.4798  | 812.480 -0.3358 | -0-2372   | 821.480 -0.1859 | -0-1335  | -0.0824  | -C.0257  | 2120 0        | 0.0885   | 0-1474   | 6.1985   | 0.3138   | 0-4718   |
| YNOL ES                              | CR PSC             | 802-706  | 812.480         | 819.287   | 821.480         | 822-841  | 823.399  | 823.333  | 822.577       | 821-187  | 819.221  | 816.498  | 808.397  | 798.244  |
| AVERAGE REYNOLIS<br>Number<br>23957. | C# H20             | 762.558  | 765.961         | 766.188   | 766.887         | 768.031  | 769-544  | 771-888  | 774-743       | 778.118  | 781.956  | 785.936  | 795.795  | 805.750  |
|                                      | C# H2G             | 764.089  | 769-392         | 114.469   | 117.557         | 786.563  | 782.551  | 792-967  | 782.684       | 786.598  | 176.175  | 173.646  | 768.625  | 162.454  |
| AVERAGE MACH<br>G.4C1                | CF HZC             | 807.272  | 197.185         | 786.195   | 784.149         | 786-415  | 177.261  | 774.270  | 771.850       | 268.963  | 768-267  | 167.502  | 766.575  | 761-745  |
|                                      | CM HZO             | 669.973  | 675.886         | 87 6. 874 | £79.917         | 660.403  | 880.750  | £80.681  | 8 A C . 4 C 3 | 879.986  | 879.222  | 876.249  | 674.843  | 169.006  |
| BETA<br>0E6<br>20.0                  | CM H20             | 884.573  | 884.364         | 884-156   | 884.225         | 684.156  | 984.260  | 951.198  | 884.190       | 884.190  | 864.225  | 864.225  | 684.503  | 884.642  |
|                                      | CM M2C             | 188.127  | 791-361         | 791.381   | 191.381         | 791.381  | 191.381  | 791.381  | 191.167       | 791.381  | 791.381  | 791.381  | 791.381  | 191-161  |
|                                      | ALPHA<br>GE G      | -20.0    | -15.6           | -10-0     | -7.5            | -5.0     | -2.5     | 0-0      | 5.5           | 5.0      | 7.5      | 10.0     | 15.0     | 20.0     |

Pressure Coefficients for the five-Perfect Confeat Probe, M. - 0.6

|       |                 | 85.TA<br>0.5.G    | <b>∢</b> ∪ | AVERAGE MACH | <b>3</b> . | AVERAGE REYNOLDS<br>NUMEER | ROLES        | AVERACE TEMPERATURE | MP ERATURE   |              |           |
|-------|-----------------|-------------------|------------|--------------|------------|----------------------------|--------------|---------------------|--------------|--------------|-----------|
|       |                 | J• J              | Ų          | 0.580        |            | 35971.                     |              | 15.2                | .2           |              |           |
| ALPHA | P.S.<br>CM H 20 | P.T.<br>C.P. H.20 | CF H 20    | CH H2C       | C# #20     | F4<br>CM H2C               | CM H2C       | (ALPHA)             | DEL TA CP    | CP (AVERAGE) | C TO TAL) |
| -20.0 | 786.211         | 986.022           | 579.613    | 653.983      | 745.989    | 7 66.060                   | 738-910      | -0.4357             | -0.0351      | 767777       | 19563     |
| -15.0 | 786.211         | 605.886           | 100.006    | 636.527      | 767.669    | 770.786                    | 760.651      | -0.3250             | -0.0335      | -6.6111      | 0.5876    |
| -10.0 | 786.211         | 987.883           | 587.675    | 619.172      | 784.659    | 777.181                    | 177.804      | -0.2082             | -6.6310      | C.016E       | 0666.3    |
| -7.5  | 786-211         | 987.744           | 452-185    | E12.113      | 789.448    | 780-077                    | 785-113      | -0.1590             | -0-0316      | C-0247       | 1.0000    |
| -5.0  | 786.211         | 987.814           | 387.814    | 804.451      | 794.194    | 784-401                    | 787.558      | -0.0955             | -6.0329      | 0-0319       | 1.0000    |
| -2.5  | 786.211         | 986-161           | 588.151    | 798.015      | 196-909    | 788.946                    | 789.750      | 6570-0-             | -0-0355      | 0.0356       | 1-0000    |
| 0-0   | 786.211         | 987.536           | 567.536    | 196-961      | 197-191    | 794-717                    | 790-715      | 6.0187              | -0.0352      | 0.0364       | 1-0000    |
| 2.5   | 735.866         | 947.261           | 587.261    | 784.786      | 756.605    | 801-029                    | 789.566      | 0.0867              | -0.0349      | 0.0354       | 1.0000    |
| 5.0   | 785.866         | 967.191           | 161.191    | 7 80 . 69 5  | 794.634    | 807.626                    | 787.495      | 0.1328              | -0.0355      | C.C338       | 1.0000    |
| 7.5   | 785.366         | 987.400           | 967.191    | 776.675      | 750.753    | 815.268                    | 763.453      | 0.1915              | -0.0362      | 0.0281       | 0.9990    |
| 10.0  | 785.866         | 987.469           | 967.191    | 173.216      | 785.504    | 822.548                    | 776-103      | 0.2447              | -0.0367      | 0.0197       | 0.9966    |
| 15.0  | 785.866         | 967.956           | 583.647    | 766.661      | 77C.C19    | 839.984                    | 762-179      | 0.3618              | -0.035A      | 2500-3-      | 6.5767    |
| 20.0  | 785.865         | 986.913           | 975.864    | 762.336      | 750.572    | 857.500                    | 744.036      | 0.4733              | -0.0325      | -0.0361      | 05450     |
|       |                 | # C               | er (       | AVERAGE PACH | <u>.</u>   | AVERAGE REYNOLDS           | SOTOR        | AVERAGE TEMPERATURE | MP ER A TURE |              |           |
|       |                 | 3                 | 9          |              |            |                            | í            | د                   | د            |              |           |
|       |                 | 2.5               | ď          | 0.586        |            | 35721•                     |              | 16.4                | 4.           |              |           |
| ALPHA | CM H 20         | CF H20            | CH H20     | CMPR         | P 3        | P4<br>CM H2C               | P5<br>CH H20 | CELTA CP            | CELTA CP     | CAVERAGES    | (TOTAL)   |
| -20.0 | 785.866         | 985.662           | 517.253    | €53.598      | 746.717    | 765.433                    | 145-403      | -0-4413             | 0.0235       | -6.0479      | 6.9579    |
| -15.0 | 785.866         | 967-191           | 985.454    | 835.720      | 762.336    | 769.818                    | 167.424      | -0-3273             | 0.0253       | -0.0101      | 0.5914    |
| -10.0 | 185.866         | 987.261           | 986.983    | 618.566      | 778.646    | 775-871                    | 783.915      | -0.2120             | C-0262       | C.0168       | 9865-0    |
| -7.5  | 786.555         | 988-436           | 586.367    | 611.573      | 785-047    | 179.758                    | 790-014      | -0.1576             | 0-0246       | 0.0250       | 1566.0    |
| -5.6  | 786.555         | 966.506           | 986.506    | 664-313      | 789-431    | 783-921                    | 793-916      | -0-1010             | 0.0222       | 0.0314       | 1.0000    |
| -2.5  | 786.555         | 987.950           | 967.950    | 197.375      | 791-804    | 788-989                    | 196.450      | -0.0416             | C-0231       | 0.0352       | 1.000     |
| 0.0   | 786-211         | 987-605           | \$87-605   | 790.836      | 1 52-304   | 793.913                    | 125.961      | 0.0153              | 0.0210       | 0-0357       | 1.0000    |
| 2.5   | 786.211         | 987.397           | 168.185    | 785.466      | 791-701    | 800-328                    | 195.924      | 0.0739              | C.0210       | C. 0355      | 1-0000    |
| 5.6   | 785.866         | 987-122           | 587.122    | 780.476      | 789.003    | 807.223                    | 792-945      | 0.1329              | 0.0196       | 0-0325       | 1.0000    |
| 7.5   | 785.866         | 986-174           | 366.496    | 116.454      | 785.061    | 814.664                    | 788.903      | 0.1962              | 0.0191       | 6923-3       | 6.5986    |
| 10.0  | 185.866         | 986-705           | 125.985    | 173-156      | 779.693    | 821-723                    | 783.714      | 0.2418              | 0-0100       | 0.0187       | 0.9991    |
| 15.0  | 785.521         | 986-062           | 982.746    | 766.778      | 164.364    | 839.015                    | 767.703      | C-36C2              | 0.0169       | -0.0053      | 0.9834    |
| 50.0  | 785-521         | 985.943           | 975.310    | 762.434      | 169.972    | 856.874                    | 746.518      | 0.4712              | 0.0191       | -0-0369      | 6946.0    |

9.0

|               |         | 8ETA<br>0.6.6 | €0            | AVERAGE PACH<br>Number | <u>.</u>     | AVERAGE REYNOLDS<br>NUMBER | ROLDS        | AVERAGE TEMPERATURE | MPERATURE<br>EG C |           |           |
|---------------|---------|---------------|---------------|------------------------|--------------|----------------------------|--------------|---------------------|-------------------|-----------|-----------|
|               |         | 5.0           | 6             | 0.58C                  |              | 35699                      | •            | 16.5                | 5.                |           |           |
| ALPHA<br>0 EG | CM H20  | CM H20        | CH H 20       | CM PZC                 | P3<br>CM H20 | CM H20                     | F5<br>CM H20 | CELTA CP<br>(ALPHA) | DELTA CP          | CAVERAGE) | (TOTAL)   |
| 0.02-         | 785.176 | 965.596       | 516.915       | 651.180                | 735.564      | 763.417                    | 753.160      | -0.4379             | 0.0878            | 9943-3-   | C-9567    |
| -15.0         | 785.176 | 986.085       | 582.610       | £33-2C1                | 756.378      | 766.272                    | 174.397      | -0.3331             | 0.0897            | -0.0130   | C.9827    |
| -10.0         | 785.176 | 986.085       | 585.737       | 817.112                | 112.446      | 772.446                    | 790-445      | -0.2223             | 0.0896            | 0.0146    | C-9983    |
| -7.5          | 785.176 | 986.G15       | 5 85 . 946    | £07.70C                | 778-540      | 176.428                    | 196.097      | -0.1557             | C-0874            | 6-6225    | 2556.3    |
| -5.0          | 185-176 | 986.915       | 586.015       | 806-521                | 732.562      | 780.591                    | 199.857      | -0.0992             | 0.0861            | 0.0284    | 1.0000    |
| -2-5          | 785.176 | 986.015       | \$86.015      | 794.226                | 784.573      | 184.975                    | 802.110      | 1340-0-             | C-0873            | 0.0313    | 1-0000    |
| 0.0           | 785-176 | 986.015       | 586.015       | 788.032                | 785.579      | 199.061                    | 802.834      | 6.0131              | C. 0859           | 0.0329    | 1.0000    |
| 2.5           | 785.176 | 986.315       | 586.015       | 782.522                | 785.136      | 797.384                    | 801.848      | 0-0140              | 0.0832            | 0.0326    | 1.0000    |
| 5.6           | 785.176 | 986.363       | 546.015       | 777.615                | 782.844      | 804.161                    | 799.254      | 0.1319              | C.0816            | C. C288   | C . 9982  |
| 7.5           | 786.555 | 986.389       | 587.672       | 114.696                | 786.391      | 812.438                    | 796.530      | C-1873              | C-0805            | 0.0220    | 0.9979    |
| 10.0          | 786.555 | 568.436       | 987.502       | 170.766                | 774.511      | 820.442                    | 790.959      | 0.2464              | C. 07 95          | 0.0134    | 6566-3    |
| 15.0          | 786.555 | 988.E45       | 585-448       | 763.790                | 755.889      | 837.657                    | 175-474      | 0.3665              | 0.0771            | -C.C114   | 2+35-3    |
| 20.0          | 786.555 | 988.575       | 976.866       | 761.578                | 739.255      | 856.962                    | 755.642      | 6.4722              | 0.0781            | -6.0413   | 0-5450    |
|               |         | 8E1A          | ح.ت           | AVERAGE MACH           | ±:           | AVERAGE REYNOLDS<br>NIMEFR | YNOLGS       | AVERACE TEMPERATURE | MPERATURE         |           |           |
|               |         | 7.5           | 2             | 0.580                  |              | 35797.                     |              | 1 91                | 16.5              |           |           |
|               |         |               |               |                        |              |                            |              |                     |                   |           |           |
| ALPHA         | CM H 20 | CM H20        | C F H 20      | CF H 2C                | CH H20       | CH H2C                     | CM H2C       | CELTA CP            | CELTA CP          | (AVERAGE) | ( TO TAL) |
| -20.0         | 786.555 | 969.131       | \$61.675      | 650.809                | 733.624      | 760.371                    | 761-296      | 7977-0-             | 0.1366            | - C. (495 | 5355.3    |
| -15.0         | 786.555 | 988.575       | 985-796       | 832-649                | 925-831      | 763.066                    | 782.533      | -0-3444             | 0.1416            | -0.C174   | 0.9862    |
| -10.0         | 786.555 | 988.575       | 587.880       | 814.469                | 770-406      | 770-688                    | 796.863      | -0.2167             | 0 - 14 10         | C.01C2    | 9956*)    |
| -1.5          | 766.555 | 984-367       | 5 P 2.089     | 806.626                | 116.037      | 774-308                    | 803-951      | -0-1601             | 0.1383            | C.C182    | 0.5986    |
| -5.0          | 186.900 | 988.712       | 5 P B . 5 7 3 | 159.561                | 786.525      | 778.655                    | 808-117      | -0.1039             | 0.1367            | 0.0239    | C-9993    |
| -2.5          | 786.906 | 568.7Pi       | 588.781       | 261.261                | 782.677      | 783.582                    | 610.329      | 9570-0-             | C-1370            | 0.0270    | 1- 6000   |
| 0.0           | 787.245 | 989-126       | 585.126       | 786.883                | 783-725      | 780-819                    | 811.216      | 0.0145              | 0.1362            | C-0281    | 1.0000    |
| 2.5           | 187.245 | 965-126       | 589.126       | 781.512                | 783-222      | 796.174                    | 810.211      | 0.0726              | 0.1337            | 0.0274    | 1.0000    |
| 5.6           | 787.569 | 963.568       | 619.618       | 111.554                | 781-194      | 803-175                    | 806.343      | 0-1265              | 0-1341            | 0.0246    | 5155.7    |
| 1.5           | 187.589 | 988.845       | 588.845       | 773.351                | 776.850      | 810.677                    | 803-115      | 0.1865              | 0.1303            | 2/13-3    | 1.600     |
| 10.0          | 187.589 | 588-984       | 988.915       | 770.153                | 7711-782     | 818.216                    | 197.966      | 0.2367              | 0.1300            | 3600°3    | 1655.3    |
| 15.0          | 187.934 | 401.696       | 546.340       | 260.297                | 757-164      | 8 16 - 40 i                | 762-363      | 0.3688              | 6.1254            | -6.6171   | 4736.5    |
| 50.0          | 187.534 | 393.390       | 511.445       | 151.567                | 736.893      | 856.290                    | 161-629      | 0064.0              | 0.1228            | 487°3-    | C.94C7    |

TABLE 4 (Cont'd)
Pressure Coefficients for the Five-Ported, Coeffel Brobe, M. - 0.6

|                              |        | CAVERAGES (TOTAL) | -0.C581 C.9456 | -0.0248 0.9855 | 5866.0 0.9982 | 0-0100 0-9993 | 0.0150 1.0000 | 0.0175 1-000 | 0.0188 1.0000 | C.C181 1.COOC | 0.0149 0.9997 | 0666 0 7600 0 | C.0017 0.9965 | -0.0237 0.5717 | +926.0 9293.7- |                            |        | CAVERAGE) (TOTAL) | -0-0717 0-9064 | -0.0375 0.9506 | -0.0216 0.97Ce | -0.0162 0.9844 | -0.0128 0.9883 | -0.0098 0.9914 | *365°3 9800°3- | -0-0092 0-9886 | -C.0137 C.9859 | -0.C199 0.979C | -0.0254 0.9697 | -C-0455 C-543E | -0.0833 0.6962 |
|------------------------------|--------|-------------------|----------------|----------------|---------------|---------------|---------------|--------------|---------------|---------------|---------------|---------------|---------------|----------------|----------------|----------------------------|--------|-------------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| MPERATURE<br>EG C            | 0.     | DELTA GP (        | 0-1903         | C.2017         | 0.2019        | 0.2011        | 0.2002        | 0.1986       | 0.1955        | 6.1939        | 6-1965        | 0.1912        | 0.1888        | 0.1822         | 0.1738         | MPERATURE                  | , ~    | DELTA CP (SETA)   | 0.2920         | 0.3237         | 0.3338         | 0.3340         | C. 3264        | 0.3187         | 0.3142         | 0.3173         | 0-3223         | 0.3230         | 0.3191         | 0.2988         | 0.2665         |
| AVERACE TEMPERATURE<br>DEG C | 17.0   | CELTA CP          | -0-4737        | -0-3357        | -0.2281       | -0-1679       | -0-10£1       | -0.0495      | 0.0116        | C.0562        | 0.1218        | 0.1755        | 0.2317        | 0.3656         | 0.5175         | AVERACE TEMPERATURE        | 15.7   | CELTA CP          | -0.5069        | -0.3469        | -0.2331        | -0.1800        | -0.1258        | -0.0687        | -0-0095        | 0.0515         | 0.1108         | 0.1729         | 0.2265         | 0.3540         | 0.5237         |
| ROLES                        |        | CM #20            | 771.676        | 788.625        | 807.556       | 815.348       | 816.968       | 818.818      | 819.180       | 818.215       | 815.862       | 611.337       | 805-545       | 189.457        | 768.703        |                            |        | CM H20            | 796.480        | 817.737        | 832.739        | 837.606        | 840.295        | 841.844        | 842.085        | 841-341        | 638.284        | 833.257        | 427.607        | 810.773        | 189-111        |
| AVERAGE REYNDLES<br>NUMBER   | 35685. | CH H20            | 751.407        | 754.836        | 765.123       | 768.542       | 772.845       | 177.172      | 785.745       | 789.758       | 796-697       | 805-676       | 811.581       | 830-643        | 850.191        | AVERAGE REYNOLDS<br>NIMFFR | 36031. | CM H20            | 738.441        | 750-266        | 154-221        | 756.842        | 758-948        | 763.533        | 769.305        | 776.283        | 783.986        | 192.674        | 801.120        | 820-858        | 840-416        |
|                              |        | CM 720            | 732.705        | 746.142        | 766.832       | 772.785       | 776.586       | 178.758      | 779.604       | 779.160       | 776.284       | 172.625       | 767.516       | 152.155        | 733-710        |                            |        | CH F20            | 137.596        | 752.216        | 765.188        | 170.597        | 774.312        | 111.570        | 178.696        | 777.369        | 173.327        | 768.698        | 763.453        | 750.562        | 7,36.042       |
| AVERAGE MACH                 | 2.586  | CP H2C            | 116.949        | 623.355        | 811.116       | 802.4CE       | 579.761       | 787.747      | 781.412       | 176.425       | 172.162       | 768.522       | 165.324       | 757.C1t        | 145.978        | AVERAGE MACH               | 6.578  | C* H2C            | 646.662        | 826.492        | 801.407        | 196.261        | 764.388        | 117.385        | 771.215        | 765.886        | 761.663        | 758.003        | 594.551        | 149.476        | 134.635        |
|                              | ٥      | P.1<br>C* H20     | 116.115        | 882.552        | 986.570       | 986.748       | 566.917       | 988.917      | 602.835       | 588-709       | 586.639       | 586.500       | 567.944       | 196.585        | 974.219        |                            |        | F1<br>CF H2G      | 195*515        | 985.189        | 589.250        | 996.262        | 591.866        | 992.005        | 591.866        | 591.588        | 596.755        | 549.573        | 789.186        | 982.286        | 972.155        |
| BETA<br>PETA                 | 16.0   | PT CM 320         | 588.917        | 174.286        | 988.917       | 988.917       | 988.917       | 988.917      | 988.709       | 986.709       | 986.709       | 988.709       | 988.639       | 988.639        | 988.996        | 95TA                       | 15.0   | CK H2C            | 994.432        | 995.197        | 995.127        | 993.390        | 994.229        | 993.743        | 593.615        | 993.882        | 903.604        | 993.812        | 993.743        | 993.404        | 993.673        |
|                              |        | PS H NO           | 787.245        | 181.796        | 167.245       | 197.245       | 787.245       | 187-245      | 187.245       | 187-245       | 197.245       | 187.245       | 181.245       | 787.245        | 187.245        |                            |        | CM H20            | 192-159        | 192.159        | 192.159        | 192-154        | 192.676        | 192.670        | 792-C7C        | 792.070        | 132.070        | 272.567        | 192.670        | 192.676        | 132.676        |
|                              |        | ALPHA<br>DEG      | -20.0          | -15.0          | -10.0         | -1.5          | -5.0          | -2.5         | 0.0           | ç•?           | 5.0           | 7.5           | 0.01          | 15.0           | 0-02           |                            |        | ALP H A<br>0 E G  | -20.0          | -15.0          | -16-0          | -7.5           | -5.0           | -2.5           | 0.0            | 5.5            | 5.0            | 1.5            | 10.0           | 15.0           | 50.0           |

| CM H2C CP<br>736-572 725<br>741-431 734<br>755-469 732<br>764-116 733<br>764-69 739<br>772-147 753<br>772-147 753<br>769-633 761<br>749-696 777  |                                      |          | ₹      | AVERAGE MACH | ı           | AVERAGE REYNOLDS<br>Number | ROLES   | AVERAGE TEMPERATURE<br>DEG C | MPERATURE<br>EG C |          |         |
|--|--------------------------------------|----------|--------|--------------|-------------|----------------------------|---------|------------------------------|-------------------|----------|---------|
| CM H2C CM H2C CM H5C CELIBAS) OFFETAS (AVERACE) (TIGAST2 272.343 815.439 -0.4946 0.4208 -0.0890 7110.572 725.343 815.439 -0.4946 0.4208 -0.0890 741.431 734.151 835.112 -0.3419 0.4690 -C.0661 755.469 732.905 850.753 -0.2462 0.4718 -0.0571 72.126 733.810 855.177 -0.2018 0.4290 -0.0571 772.126 739.266 858.119 -0.0857 0.4290 -0.0641 772.126 739.266 858.119 -0.0857 0.4290 -0.0436 772.147 753.182 855.631 0.0401 0.4194 -0.0436 772.147 753.182 855.631 0.0401 0.4194 -0.0650 759.633 761.025 852.931 0.0966 0.4145 -0.0650 759.639 769.633 761.025 842.002 0.2076 0.4570 -0.0639 737.126 796.713 825.472 C.3163 0.4384 -0.0639 724.456 819.941 803.028 0.4936 0.3990 -0.1083  | 0.02                                 |          | •      | 675-0        |             | 35853.                     |         | 9 7                          | ٠.                |          |         |
| 7:16.572         725.343         815.439         -0.4946         0.4208         -0.0890           741.431         734.151         836.112         -0.3419         0.4690         -C.0661           755.469         732.905         850.753         -0.24E2         0.4718         -0.0571           764.116         733.810         855.177         -0.2018         0.4290         -0.0571           764.126         735.266         856.631         -0.1439         0.4249         -0.0541           772.126         739.266         858.119         -0.0857         0.4249         -0.0441           772.147         753.182         856.631         0.0401         0.4249         -0.0436           772.147         753.182         856.631         0.0401         0.4194         -0.0436           769.633         761.025         852.931         0.0401         0.4194         -0.0456           749.8%6         777.850         842.002         0.2076         0.4570         -0.0639           737.126         796.713         825.472         0.4184         -0.0639           724.456         819.941         863.002         0.3990         -0.01083                              | A 19 CM H20 CM H20 CM                | CH H20   | * 3    | CM H2E       | CH H2C      |                            | CH HZC  | CELTA CP                     | DELTA CP          | CAVERAGE |         |
| 741-43         734-151         835-112         -0.3419         0.4690         -C.0661           755-469         732-905         850.753         -0.24E2         0.4718         -0.0571           764.116         733.810         855-177         -0.2018         0.4511         -0.0571           772.126         735.063         856.631         -0.1439         0.4249         -0.0541           772.126         735.061         857.878         -0.0230         0.4229         -0.0436           772.147         753.182         856.631         0.0401         0.4223         -0.0436           769.633         761.025         852.931         0.0401         0.4194         -0.0426           769.633         761.025         852.931         0.0406         0.4194         -0.0456           769.633         769.547         647.676         0.1568         0.4405         -0.0552           749.696         777.850         842.002         0.2076         0.4570         -0.0639           737.126         796.713         825.472         0.4184         -0.0639         -0.0639           724.456         819.941         803.936         -0.0639         -0.0639         -0.0639 | 7.1 493.745 564.625 825.092          | 529.195  | 825.0  | 9.5          | 736-572     | 725.343                    | 815.439 | 9767-0-                      | 0.4208            | 0.0890-  | C. 8556 |
| 755.469         732.905         850.753         -0.24£2         0.4718         -0.0571           764.116         733.810         855.177         -0.2018         0.4511         -0.0503           764.116         733.810         855.177         -0.2018         0.4511         -0.0503           772.126         739.266         858.119         -0.0857         0.4249         -0.0441           772.147         753.182         856.631         0.00230         0.4223         -0.0435           769.633         761.025         852.931         0.0041         0.4194         -0.0426           769.633         761.025         852.931         0.0966         0.4145         -0.0456           769.635         769.547         647.676         0.1568         0.4405         -0.0552           749.696         777.850         842.002         0.2076         0.4570         -0.0639           737.126         796.713         825.472         0.3900         -0.1083           724.456         819.941         813.026         0.4836         -0.0639   | ·c 993.951 975.257 803.171           | 575.257  | 803.1  | 7.1          | 761.431     | 7 34 . 151                 | 836.112 | -0.3419                      | 0.4690            | -0.0661  | 7205-0  |
| 764.116         733.810         855.177         -0.2018         0.4511         -0.6503           769.854         735.063         856.631         -0.1439         0.4290         -0.641           772.126         739.266         858.119         -0.0857         0.4249         -0.0436           772.170         745.661         857.878         -0.0230         0.4223         -0.0436           772.147         753.182         856.631         0.0401         0.4194         -0.0426           769.633         761.025         852.931         0.0966         0.4145         -0.0456           749.8%6         777.850         842.002         0.2076         0.4570         -0.0552           737.126         796.713         825.472         6.3163         0.4384         -0.0639           724.456         819.941         863.022         0.4836         0.4384         -0.0686   | **:. CF3 994.021 \$82.276 783.C2C    | \$82.276 | 783.62 | ن            | 155.469     | 132.905                    | 850-753 | -0.2462                      | 0.4718            | -0-0571  | 0.9418  |
| 769.854         735.063         856.631         -0.1439         0.4290         -0.0441           772.126         739.266         858.119         -0.0857         0.4249         -0.0436           772.126         745.661         857.878         -0.0230         0.4223         -0.0436           772.147         753.182         856.631         0.0401         0.4194         -0.0426           769.633         761.025         852.931         0.0966         0.4145         -0.0456           758.589         769.547         847.676         0.1568         0.4405         -0.0552           749.896         777.850         842.002         0.2076         0.4570         -0.0539           737.126         796.713         825.472         6.3163         0.4384         -0.0666           724.456         819.941         803.028         0.4836         -0.0686         -0.0686  | 11,110 591,917 584,222 774,514       | 584.222  | 174.53 | <b>.</b>     | 764.116     | 733-810                    | 855-177 | -0.2018                      | 0.4511            | -0.0503  | 6.9526  |
| 772.126 739.266 858.119 -0.0857 0.4224 -0.0436<br>772.170 745.661 857.878 -0.0230 0.4223 -0.0432<br>772.147 753.182 856.631 0.0401 0.4194 -0.0426<br>769.633 761.025 852.931 0.0966 0.4145 -0.0426<br>758.989 769.547 647.676 0.1568 0.4405 -0.0552<br>749.696 777.850 842.002 0.2076 0.4570 -0.0639<br>737.126 796.713 825.472 0.3163 0.4384 -0.0866  | 7+3.147 992.645 983.541 764.183      | 583-541  | 764.18 | <b>~</b> ,   | 768.854     | 735-063                    | 856.631 | -0-1439                      | 0.4290            | 1440-0-  | 0.9550  |
| 772-170 745-661 857-878 -0.0230 0.4223 -0.0432<br>772-147 753-182 856-631 0.0401 0.4194 -0.0426<br>769-633 761-025 852-931 0.0966 0.4145 -0.0426<br>758-989 769-547 647-676 0.1568 0.4405 -0.0552<br>749-896 777-850 842-002 0.2076 0.4570 -0.0639<br>737-126 796-713 825-472 0.3163 0.4584 -0.0866<br>724-456 819-941 803-002   | 14 992.714 984.861 756.601           | 984-861  | 756.60 | =            | 772.126     | 739.266                    | 858.119 |                              | 0.4249            | -0.0436  | 0.9612  |
| 772-147 753-182 856-631 0.0401 0.4194 -0.0426 769-633 761-025 852-931 0.0966 0.4145 -0.0450 758-989 769-547 647-676 0.1569 0.4405 -0.0552 749-896 777-850 842-002 0.2076 0.4570 -0.0639 737-126 796-713 825-472 0.3163 0.4384 -0.0866 724-456 819-941 803-029 0.4836 0.3900 -0.1083  | 743.547 991.880 984.236 750.286      | 984.236  | 750.28 | 9            | 172.170     | 145.661                    | 857.878 | -0.0230                      | 0.4223            | -0.0432  | 0.9621  |
| 769.633 761.025 852.931 0.0966 0.4145 -C.0450<br>758.989 769.547 647.676 0.1568 0.4405 -0.0552<br>749.8%6 777.850 842.002 0.2076 0.4570 -0.0639<br>737.126 796.713 825.472 0.3163 0.4384 -0.0866<br>724.456 819.941 803.000 0.4836 0.3900 -0.1083  | 790.347 991.776 983.437 745.098      | 983.437  | 745.0  | 8 6          | 772.147     | 753.182                    | 856.631 | 0-0401                       | 0.4194            | -0-0426  | 0.9586  |
| 758.989 769.547 647.676 0.1568 0.4405 -0.0552<br>749.8%6 777.850 842.002 0.2076 0.4570 -0.0639<br>737.126 796.713 825.472 0.3163 0.4384 -0.0805<br>724.456 819.941 803.08 0.4836 0.3900 -0.1083  | 790.147 991.290 982.012 741.619      | 582.012  | 741-61 | 6            | 769.633     | 761-025                    | 852.931 | 0.0966                       | 0.4145            | -6.0450  | 0.9538  |
| 749-8%6 777-850 842-002 0-2076 0-4570 -0.0639<br>737-126 796-713 825-472 C-3163 0-4364 -0.0806<br>724-456 819-941 803-000 0-4836 0-3900 -0.1083  | 189.657 990.983 979.724 737.973      | 428-615  | 137.91 | ٠,           | 758.589     | 169.547                    | 947-676 | 0-1568                       | 0 -4405           | -0.0552  | 3.9441  |
| 737.126 796.713 825-472 6.3163 0.4384 -0.6866<br>724.456 819.941 863.688 0.4836 0.3900 -0.1083   | 1 ) 789.313 990.846 977.364 736.019  | 977.364  | 736.01 | <b>5</b>     | 749.856     | 777.850                    | 842-002 | 0.2076                       | 0.4570            | -0.0639  | 0.9331  |
| 724.456 819.941 8C3.C88 0.4836 0.3900 -0.1083  | 11.0 789.313 990.646 970.415 732.963 | 570-415  | 132.96 | m            | 7 37 - 1 26 | 796.713                    | 825-472 | 6-3163                       | 0.4384            | 9080-0-  | 6.8986  |
|  | 20.0 789.313 990.916 959.678 722.445 | 959-678  | 122.44 | Ŋ            | 124-456     | 819-941                    | 863.688 | 0.4836                       | 0 - 3 0 0 0       | -0.1083  | 0.8451  |

TABLE 4

Pressure Coefficients for the Five-Ported, Conical Probe, 0.12  $\leq M_{\omega} \leq 0.61$ 

| ALPHA BETA DEG DEG 0.0 0.0 | CP (TOTAL)          | 0.9995  | 9666 0   | 1-0000  | 0.9989  | 0.9979  | 0.9976  | 0.9974  | 0.9969 | 9966 0 | 0.9957 | 0.9950  | 0.9950  | 0.9954  | 0.9931  | 0,9918  | 9066 0  | 0.9876  | 0.9875  | 0.9866  | 0.9857  | 0-9826  |
|----------------------------|---------------------|---------|----------|---------|---------|---------|---------|---------|--------|--------|--------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
|                            | CP<br>(AVERAGE)     | 0.0490  | 0.0484   | 0.0480  | 0-0460  | 0.0437  | 0.0427  | 0.0460  | 0.0443 | 0.0423 | 0.0433 | 0.0430  | 0.0410  | 0.0409  | 0.0441  | 0.0425  | 0.0406  | 0.0416  | 0.0425  | 0.0427  | 0.0426  | 0-0401  |
|                            | DELTA CP<br>(BETA)  | -0*0001 | 0.0001   | 000000  | -C.00C1 | 00000-0 | -0.0001 | 0000-0- | 0.0010 | 0.0021 | 600000 | 0.0022  | 0.0032  | 0~0050  | 9000*0- | 0.000   | 0.0013  | 0.000   | -0.0003 | 1100-0- | -0.0024 | C-0023  |
|                            | DELTA CP<br>(ALPHA) | 000000  | 10000-0- | -0.0001 | -0*0001 | 0-0002  | 600000  | 0.0010  | 0.0016 | 0.0015 | 0.0005 | 0.0003  | -0-0005 | -0.0013 | 4000-0  | -0*0005 | -0.0018 | -0.0012 | 6000*0- | 0-0038  | 0.0040  | -0.0023 |
|                            | P5<br>C# H20        | 773.88  | 773.82   | 773.98  | 774.11  | 774.40  | 774.64  | 774.72  | 774.47 | 774.29 | 775.23 | 775-19  | 775.03  | 776.09  | 778.73  | 778.10  | 177.92  | 778.69  | 779.39  | 780.52  | 782.49  | 781.64  |
|                            | P4<br>CM H20        | 173.84  | 773.95   | 774.02  | 114-11  | 174.37  | 174.32  | 14-61   | 774.34 | 774-53 | 775.33 | 776.02  | 776.58  | 49-117  | 778.06  | 778.83  | 779-81  | 179.67  | 780.38  | 178.69  | 178.41  | 785.16  |
|                            | P3<br>CM H20        | 173.81  | 773.94   | 174.01  | 774.04  | 774.43  | 774.57  | 174.71  | 775.26 | 775.99 | 775.95 | 177.04  | 177.78  | 777.85  | 778.20  | 778.80  | 119.11  | 779.39  | 779.11  | 779.53  | 780.24  | 783.89  |
|                            | P2<br>CM H20        | 73.87   | 143.61   | 773.96  | 173.99  | 774.54  | 775.03  | 115.41  | 175.60 | 175.74 | 175.74 | 176.30  | 776.16  | 176.51  | 178.41  | 178.62  | 778.20  | 778.55  | 779.53  | 782.21  | 782.21  | 782.91  |
|                            | P1<br>CM H20        | 780.87  | 782-14   | 784.03  | 785.93  | 795.21  | 800.49  | 803-44  | 805.76 | 812.51 | 821.37 | 835-08  | 944.16  | 859.98  | 883.81  | 893.52  | 903.43  | 907-86  | 917-36  | 931.70  | 946.05  | 975.58  |
|                            | TOTAL<br>TEMP (CJ   | 7.0     | 0.9      | 0.9     | 0-9     | 0.9     | 7.0     | 9.0     | 2.6    | 5.0    | 0-+    | 9.4     | 4.0     | 3.0     | 0.4     | 3.0     | 0.4     | 3.0     | 3•0     | 3.0     | 2-0     | 3.0     |
|                            | PT<br>CM H2C        | 781.29  | 782.56   | 784-03  | 7 86.76 | 26-952  | 8 62-35 | 8 05.55 | 808.25 | 815.26 | 824.96 | 8 39.30 | 848.37  | 863.99  | 889.93  | 36-036  | 912.06  | 919-25  | 958.96  | 944.36  | 9 59.76 | 992-86  |
|                            | P.S<br>CM H20       | 773.5   | 773.5    | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5  | 773.5  | 773.5  | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   | 773.5   |
|                            | REYNOLDS<br>NUMBER  | 7187.   | 7759.    | 8364.   | 9383.   | 12427.  | 13763.  | 14461.  | 15139. | 16558. | 18375. | 20713.  | 22052.  | 24204-  | 27258.  | 28500.  | 29603.  | 30370.  | 31304.  | 32718.  | 34119.  | 36727.  |
|                            | MACH                | 0.120   | 0.129    | 0-139   | 0.156   | 0.207   | 0.230   | 0.242   | 0-252  | 0.275  | 0.305  | 0.344   | 0.366   | 0-401   | 0.452   | 0.472   | 164.0   | 0-503   | 0.518   | 0.542   | 0.564   | 0.608   |

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